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ENHANCED EXTREME LEARNING MACHINE FOR GENERAL REGRESSION AND CLASSIFICATION TASKS

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By

SAIF F MAHMOOD

Thesis Submitted to the School of Graduate Studies, Universiti Putra Malaysia, in Fulfilment of the Requirements for the Degree of Doctor of Philosophy

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DEDICATION

Dedicated to:

My family.



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfilment of the requirement for the degree of Doctor of Philosophy

ENHANCED EXTREME LEARNING MACHINE FOR GENERAL REGRESSION AND CLASSIFICATION TASKS

By

SAIF F MAHMOOD



Chairman : Professor Mohammad Hamiruce Marhaban, PhD Faculty : Engineering

Extreme Learning Machine (ELM) is a single hidden layer feedforward neural network which randomly chooses hidden nodes and analytically determines the output weights using least square method. Despite its popularity, ELM has a number of challenges worth to investigating for improving the usability of ELM in a more advanced application. This thesis focusses on challenges namely design architecture and learning technique. The first challenge is to select the optimal number of hidden nodes for ELM in different application. To address this problem, a new approach referred to SVM-ELM is proposed, which utilizes 1-norm support vector machine (SVM) to the hidden layer matrix of ELM in order to automatically discover the optimal number of hidden nodes. The method is developed for regression task by using mean/ median of ELM training errors which is then used as threshold for separating the training data and converting the continuous targets to binary. This will allow projection to 1norm SVM dimension in order to find the best number of nodes as support vectors. Second problem in ELM, is the restriction in performance of ELM in terms of training time and model generalization, due to the complexity of singular value decomposition (SVD) for computing the Moore-Penrose generalized inverse of the hidden layer matrix, especially on a large matrix. To address this issue, a fast adaptive shrinkage/thresholding algorithm ELM (FASTA-ELM) which uses an extension of forward-backward splitting (FBS) to compute the smallest norm of the output weights in ELM is presented. The proposed FASTA-ELM replaces the analytical step usually solved by SVD with an approximate solution through proximal gradient method, which dramatically speeds up the training time and improves the generalization ability in classification task. The performance of FASTA-ELM is evaluated on face gender recognition problem and the result is comparable to other state-of-theart methods, with significantly reduced training time. For instance, the training



time of 1000 nodes ELM is 18.11 s, while FASTA-ELM completed in 1.671 s. The proposed modification to the ELM shows significant improvement to the conventional ELM in terms of training time and accuracy, and provide good generalization performance in regression and classification tasks.



Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia sebagai memenuhi keperluan untuk ijazah Doktor Falsafah

MESIN PEMBELAJARAN EKSTRIM DIPERTINGKAT UNTUK TUGASAN REGRESI UMUM DAN PENGELASAN

Oleh

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September 2020

Pengerusi : Profesor Mohammad Hamiruce Marhaban, PhD Fakulti : Kejuteraan

Mesin pembelajaran ekstrim (*Extreme Learning Machine*: ELM) adalah satu rangkaian neural lapisan tersembunyi tunggal suap ke depan, yang memilih nod tersembunyi secara rawak dan menentukan pemberat keluaran secara analitik dengan menggunakan kaedah kuasa dua terkecil. Walaupun begitu, mempunyai cabaran yang perlu dikaji untuk meningkatkan ELM kebolehgunaan ELM dalam aplikasi termaju. Thesis ini memberi tumpuan kepada dua cabaran utama iaitu reka bentuk seni bina dan teknik pembelajaran. Cabaran pertama adalah memilih bilangan nod tersembunyi yang optimum untuk ELM dalam pelbagai aplikasi. Untuk mengatasi masalah ini, pendekatan baru yang dinamakan sebagai SVM-ELM dicadangkan, yang menggunakan mesin vektor sokongan (Support Vector Machine: SVM) 1norma terhadap lapisan tersembunyi matriks ELM untuk secara automatik mendapatkan bilangan nod tersembunyi yang optimum. Kaedah ini dibangunkan untuk tugasan regresi dengan menggunakan purata atau median ralat latihan ELM yang mana seterusnya ia digunakan sebagai titik ambang untuk memisahkan data latihan dan menukar sasaran berterusan ke binari. Ini membolehkan unjuran ke dimensi SVM 1-norma untuk mencari bilangan nod terbaik sebagai vektor sokongan. Masalah kedua dalam ELM adalah prestasi ELM yang terhad dari segi tempoh latihan dan generalisasi model, disebabkan kerumitan penguraian nilai tunggal (Singular Value Decomposition: SVD) untuk mengira pembalikan umum Moore-Penrose dari matriks lapisan tersembunyi, terutama bagi matriks yang besar. Untuk mengatasi masalah tersebut, algoritma penyusutan / titik ambang tersuai pantas (Fast Adaptive Shrinkage/Tresholding Algorithm: FASTA) ELM (FASTA-ELM) yang menggunakan lanjutan pemisahan maju-mundur (Forward-Backward Splitting: FBS) untuk mengira norma terkecil dari pemberat keluaran ELM dipersembahkan. FASTA-ELM yang dicadangkan menggantikan langkah analitik yang biasanya diselesaikan oleh SVD dengan



penyelesaian hampiran melalui kaedah kecerunan proksimal, yang terbukti mempercepat tempoh latihan dan meningkatkan kemampuan generalisasi dalam tugasan pengkelasan. Prestasi FASTA-ELM dinilai berdasarkan masalah pengecaman jantina dan hasilnya setanding dengan kaedah terkini, dengan tempoh latihan yang lebih pantas. Sebagai contoh tempoh latihan untuk 1000 nod ELM adalah 18.11 s, sementara FASTA-ELM selesai dalam 1.671 s. Pengubahsuaian ELM yang dicadangkan menunjukkan peningkatan signifikan ELM konvensional dari segi tempoh latihan dan kejituan, dan memberi prestasi generalisasi yang baik dalam tugasan regresi dan pengkelasan.



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LIST OF ABBREVIATIONS

	ELM	Extreme Leaning Machine
	LBP	Local Binary Pattern
	HOG	Histogram of Oriented Gradients
	WLD	Weber Law Descriptor
	SVM	Support Vector Machine
	TP	True Positive
	TN	True Negative
	SLFN	Single Layer Feedforward Network
	FASTA	Fast Adaptive Shrinkage / Thresholding Algorithm
	S-ELM	Standard Extreme Leaning Machine
	EM-ELM	Error minimized Extreme Leaning Machine
	R-ELM	Regularized Extreme Leaning Machine
	SVD	singular Value Decomposition
	BP	Back Propagation
	RBF	Radial Basis Function
	OP-ELM	Optimally Pruned Extreme Learning Machine
	BIP-ELM	Batch Intrinsic Plasticity Extreme Learning Machine
	EAs	Evolutionary Algorithms
	RVFL	Random Vector functional-link
	VC dimension	Vapnik–Chervonenkis dimension
	LS-SVM	Least Square Support Vector Machine

CHAPTER 1

INTRODUCTION

In general, this chapter introduce background knowledge on the domain of machine learning approach. More insight is given into Artificial Neural Network (ANN) method, with highlights to the tendency of initial weight by random process in a method knowing as Extreme Learning Machine (ELM). In addition, this chapter points out the problem statement, objectives that are to be achieved at the end of this study, and, the scope of the research.

1.1 Machine Learning Approach

In recent years, in line with technological advances, machine learning has exhibited several promising algorithms in various real world applications. Rather than inference based rules, machine learning makes sense of the data through building a predication model from seen data in phase named training process, then valid the model in unseen data in second stage called testing phase. Whether the output is labelled entirely or semi and neither without labeling, data-driven tasks are learned as supervised, semi supervised and unsupervised learning respectively. Distinguished machine learning approaches lies in two important aspects include learning speed and performance. Whereas learning speed is typically depend on computational burden in term of execution time, the performance of learning algorithm is represented by generalization ability measured by training and testing error. And with incorporation of learnable functions to undertake the universality capability (universal function approximation). In addition to former two metrics, reliability of the model possess a crucial role in data-driven model as explicitly studied by Neumann (2013). To build a compact model, model parameter can be involve in optimization problem with some objective function. From particular point of view, many challenges are arisen in machine learning starting with the unpredictable model come out with complex environments and not ending up with the enormous growth in amount of data. For these, machine learning model that can be sorted include probabilistic model, geometric model and logic model (Flach 2012).

The importance of probabilistic in machine learning lies in alleviating the tendency of uncertainty by learning process. Motivated by geometric concept such as line, plane and distance, geometric model has been developed especially with high dimension with prefixed "Hyper". In additional, logic model has been used based on logical relation. Features also called attributes are contributed in the model assessment based on scale and ordering through those with numerical scale called quantitative feature and those without scale named ordinal feature as well categorical features that are without scale or ordering (Flach 2012). Basically, machine learning scheme can be

represented as shown in Figure1.1. Where the model in task box perform a mapping from date defined by features to output. Mapping is obtained using training data in learning process.



1.2 Artificial Neural Networks

The underlying function of human in brain has received considerable attention by neurologists, physiologists and psychologists. Brain architecture constitutes of immense number of computing units (neurons) that are interconnected (synapses) and operating in parallel manner. Inspired by theoretical and empirical aspects of human brain, well-known artificial neural network has been acquired as artificial brain models to solving specific problem. Basically, the main research that interested on artificial neural networks are: (i) mathematic at intrinsic of neuron and synapses; and (ii) using artificial neural networks to effectively build a machine learning model to perform data processing, inferring decisions and interpretable by simulate the biological nervous system. Indeed, two important features of neural network as a computational method (Daniel Graupe 2013):

- (i) It employs simple computational operations to solve mathematical problems with ill-define nonlinear and stochastic approach.
- (ii) It possesses a self-organizing feature with learning ability that implies the capability of solving wide range of problems.

Furthermore, White (1989) suggested QuickNet algorithm which inserted randomness of hidden neurons in the single of hidden layer feedforward networks (SLFNs) and the output of hidden layer weights can be calculated of

the current hidden neurons after adding new hidden neuron. Randomness clearly exploited in hidden neurons by Schmidt and Kraaijveld (1992).

And they concluded that output weight has significantly contributed in learning process rather than hidden layer weights. The main constraint with it is required a output neuron bias, and cannot prove the universal capability of the method. For same purpose, a new approach named Random Vector Functional Link (RVFL) which is depend on randomness that is partial technique in neurons that are hidden (Pao et al 1994) (Igelnik. B and Pao. Y. H, 1995). Although it is remarkable contribution, there is no universal capability prove of the single layer feedforward. In addition, RVFL network employed the traditional gradient descent mechanism to learn the weights of output layer, in summarize, RVFL don't exploit random features and random hidden layer neurons.

1.3 Extreme Learning Machines

The advantage of random process approach has involved a lot of consideration in many challenging of application fields, incorporation of random projections, efficient processing can be obtained for large and highdimensional data sets (Miche et al 2009). Inspired by vast literature of these methods, researchers explore the usefulness of generate the initial parameters randomly and restrict learning phase to be formalized as a linear model. A prominent machine learning method with single hidden layer feedforward neural network (SLFN) and high-dimensional random process named extreme learning machine (ELM) is suggest by Guang Bin Huang (2014a).

Compared to conventional backpropagation training methods, ELM is trained much faster with capability to be trapped at global optimum. As theoretical aspects have reveal that although that random process of hidden nodes parameters, ELM can be maintained the universal approximation capability of SLFNs. Unlike other learning process involve with random projection for /network, the indecency of hidden nodes in ELM are not only for training data but also on each other. Moreover, the generation of hidden node parameters in ELM can be obtained even before training data has been shown (Ding, Xu, & Nie, 2013). In ELM theory the meaning of random hidden nodes imply that parameters linked the hidden layer with input layer are selected by random process and without depending on the training samples, e.g., input weights are randomly generated weight and biases for additive hidden nodes such sigmoid, or both center and impact factor for RBF networks. The main aspect of ELM is the hidden nodes do not essential to be tuned (Guang-Bin Huang, Hongming Zhou, Xiaojian Ding, & Rui Zhang, 2012a). In summary, the randomness of ELM clarify in two folds:



- (a) The randomness of hidden nodes parameters.
- (b) Although the hidden nodes are randomly found, they do no need to be explicitly tuned.

For instance, a hidden node in the follow layer can be basically linear sum or nonlinear transform of some random nodes in the earlier layer. In this example, some neuron are selected randomly and some are not, but no one of them have being tuned. Different from Schmidt et al (1992) and Pao et al (1994) that each neuron is either sigmoid or RBF node only, each hidden node in ELM can be any bounded nonconstant piecewise continuous functions. As shown in Figure 1.2 ELM can be a subnetwork of other nodes in which feature learning allow to be used considerably. As well, ELM can cooperate with compression, feature learning, clustering, regression or classification, thus, homogeneous ordered blocks of ELM can be constructed. For instance, one ELM as feature learning process, the following ELM mechanism is as a classifier. In this instance, there are two hidden layers of ELM, in general it is not randomly generated and it is ordered, but hidden nodes in each layer do not need to be tuned (e.g., randomly chosen or obviously given/calculate) (Guang-bin Huang, 2015) Based on ELM theory, ELM SLFNs, activation function contains but are not restricted to:

- 1. Sigmoid activation function networks
- 2. RBF activation function networks
- 3. Threshold function networks
- 4. Trigonometric function networks
- 5. Inference Fuzzy systems
- 6. Fully complex neural networks
- 7. High-order networks
- 8. Ridge function polynomial networks
- 9. Wavelet function networks
- 10. Fourier series



Furthermore, there are distinction and similarity among ELM and other wellknown algorithms, such as Deep Learning and support vector machine (SVM) least square support vector machine (LS-SVM). Unlike deep Learning, ELM in its logic that hidden layer node of the whole ELM need not to be tuned. Because of ELM's altered roles of feature learning and clustering, ELM can be executed as the earlier layers in multilayer networks in which the late layers are trained by other learning algorithms such as deep learning.

Compared with SVM and LS-SVM, SVM was firstly found to interact with multilayer feedforward networks by Cortes and Vapnik (1995) which shows that there is no method to train a multilayer network. Different from ELM and deep learning which investigate feature representations in each layer, SVM and LS-SVM do not consider the feature representation and functioning roles of each inner hidden layer. Moreover, SVM and LS-SVM can be able as single hidden- layer networks associated with hidden layer output function. For this regard, while ELM and SVM/LSSVM possess a single hidden layers, but ELM explicitly possess hidden layer mapping (suitable for feature representations) and SVM/LS-SVM has unknown hidden layer mapping (inconvenient for feature representations). In different machine learning tasks, ELM represents feature mapping, clustering based regression and pattern classification with ridge regression optimization criteria, whereas SVM/LS-SVM basically perform for binary pattern classification based on Vapnik–Chervonenkis dimension (VC dimension) through maximal margin. However, it is hard for

SVM/LSSVM to have feature mapping because anonymous mapping as SVM and LS-SVM generally offer suboptimal results.

Moreover, the universal approximation capability of ELM can be contributed in a varied sort of functions that are nonlinear piecewise continuous, and it obvious that not need to bias existing in the output layer. For that, ELM is employed wide range of activation functions in both real and complex domains (Huang et al 2006)

Following the Bartlett's concept (Bartlett 1998), smallest training error can be associated with improving of generalization performance for the network, the proposed solution of ELM in this thesis is to solve the linear equation and reach solution of norm to be smallest. Three vital aspects making it stimulating solution (Huang et al 2006):

- 1. The minimum training error can be obtained as it is basically linear equation that use least-squares method as a solution.
- 2. Among the least-squares solutions, ELM can reach the smallest norm.
- 3. The smallest norm solution is unique among the least-squares solutions.

1.4 Problems and Motivations

Artificial Neural Networks of (ANNs) are common approaches for pattern recognition tasks. They have the ability to handle the problems in practical applications such as non-linear and noisy data. Nevertheless, it suffer from slowing of the learning in feedforward neural networks and generally far slower than necessary. Thus, it has been a main restriction for their implementations. Two important reasons could be (Zhang et al., 2008):

- (i) The slowing of the training in error back-propagation (BP) process and other gradient descent learning methods has been extensively used.
- (ii) Iteratively tune the synaptic parameters of the neural networks by using gradient descent learning algorithms.

To cope with the shortcomings mentioned above, in 2006 Huang et al (2006) suggest a novel learning algorithm called ELM for single hidden layer feedforward neural network (SLFN). ELM mitigates the iterative procedures of adjusting weights by randomly select hidden layer neurons and determine the output weights analytically. From theory point of view, ELM incline to include perfect generalization performance associated with extremely fast learning speed. Despite of many aspects on ELM, there are some basic matters that need to be studied to understand the feasibility of ELM in real-world

implementations. One of these issues is how to find the optimal and the compact network architecture, which can finally result in a robust model and applicable to many learning tasks (X. Wang & Cao, 2018). It is obvious that the choosing of an optimal number of nodes is thoroughly related to the problem of curve fitting using polynomials (Kwok & Yeung, 1997)(Rocha & Ananda, 2017). Such as too many coefficients will encounter overfitting the model and therefore poor performance would be occurred, while few coefficients cannot learn well the underlying function (MLD Dias et al. 2018). Practically, a certain number of the hidden nodes in such networks may have a minor effect on the output of the network and theoretically increase the network complexity (Guang Bin Huang et al 2004).

Moreover, ELM may meet the singularity problem in case of the number of nodes are greater than the training samples which eventually lead to instability of the system (Alcin et al., 2015). For that reason, empirical method such as trial-and-error is used to find a compact network structure for a specific task without any prior knowledge (Guang-Bin Huang et al., 2012a). ELM methods generally need a lot of hidden nodes as mentioned in (Guang-Bin Huang et al (2012a) in order to find an optimal number of neurons, publications are suggested using optimization algorithms (Sheela & Deepa, 2013).

These works also imply that identification of hidden nodes can be considered as a kind of optimization process (Rong et al., 2008). If some optimal neurons are selected in the learning process, the learning effectiveness will be improved dramatically. While reducing the number of hidden nodes can be further occur without disturbing learning performance for large-size or high dimension data sets. Guang-Bin Huang et al (2012b) has stated that good performance can be obtained as long as number of node is large enough.

Another shortcoming of ELM is the computational time during training phase due to singular value decomposition (SVD) for calculating the Moore-Penrose generalized inverse of the hidden layer matrix that has high complexity burden. Especially with large dimension on hidden layer matrix and the effect of the ill conditioned of the hidden layer matrix that make ELM suffer from quite weak numerical stability that lead to waning of the generalization performance (Tang & Han, 2009).

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According to previous explanation, the problem statement can be summarized as follow:

1. The existing methods to determine the optimal number of hidden neurons in ELM is trial-and-error approach that it is time consuming and there is no guarantee of fixing the hidden neuron.

2. The output weight of ELM is found out by using SVD which has high burden of computational complexity $0(4Nn^2 + 8n^3)$, when number hidden neurons became large the computational complexity of SVD will significantly rise.

1.5 Objectives(s) of the study

The main objective of this research work is to design, develop, and enhance ELM based neural network models that capitalize the advantage of ELM, and at the same time, avoid their limitation. To attain the main objectives, sub-objectives are defined as below:

- 1. To develop novel architectures of ELM based SVM to select the optimal number of nodes
- 2. To test and evaluate the procedure of an SVM-ELM algorithm by mitigating the influence of large number of node in regression task.
- 3. To develop a novel method named Fast Adaptive Shrinkage /Thresholding Algorithm (FASTA) to calculate the output weights of ELM with the smallest norm using a forward backward splitting.
- 4. To investigate the feasibility and efficiency of FASTA-ELM algorithm by applying it in face gender recognition task.

1.6 Research Scopes

With a single hidden layer feedforward, ELM consider the mainstay of this thesis that establish by developing a novel pruning network architectures method named ELM-SVM. As well, new learning algorithms called fast adaptive shrinkage/thresholding algorithm (FASTA-ELM) that attempt to disregards the need of employ SVD to compute the hidden layer of matrix of ELM. The scope of this research is motived on two areas:

- 1. Development of effective novel pruning strategy of network architectures systems of ELM based 1-norm SVM that are capable of acquiring the active nodes with as little supervision as possible to data regression tasks.
- 2. Development a new method that calculating the output weights of ELM with the smallest norm using a forward backward splitting method named (FASTA) for pattern classification tasks.
- 3. To demonstrate the performance of the proposed method, the dataset is used in this thesis is as follow:

For regression task, the proposed SVM–ELM is evaluated on 10 real-world regression problems from an UCI ML (C. Blake & C. Merz 1998). For

classification task, the experiments in this thesis are conducted on 5 benchmarked face gender recognition datasets as follow:

- 2 unconstrained datasets: Cropped Labeled Faces in the Wild (G. B. Huang et al., 2008) and Image of Groups(Gallagher & Chen, 2009)
- 3 constrained datasets: PAL (Minear & Park, 2004), FERET (Phillips et al., 1999), and CAS-PEAL R1 (Gao et al., 2008)
- 4. All the simulations for ELM and the new ELM algorithms are both carried out in the Matlab 2016 environment running in Intel Core i5 6200u CPU.With the speed 2.40GHz.

It is very clear that the hidden node choosing is a stimulating problem and is still a very much open problem of research. Our study in this thesis is motivated by the model suggested by Han and Yin (2008), where a 1-norm support vector machine (SVM) is used to pre-select the hidden neurons, followed by a stepwise selection method based on ridge regression for selecting the optimal hidden nodes of wavelet networks. The key objective of the proposed method is to remove the issue of including a great number of inactive neurons in wavelet networks.

Another problem in ELM that handle by this thesis that has been formulated as objective function of ELM to minimizing compound optimization problem solved with the forward backward splitting (gradient descent method) in instead of computing the hidden layer matrix analytically using SVD. However, adaptive stepsize selection method and non-monotonic line search are used in the suggested FASTA-ELM method to speed up the convergence rate. Thus, if we have a large ill-conditioned matrix, rather than searching through all possible steps of the objective, the step-size adaptively choose such as that the dimension of the gradient descent problem becomes very small, which in turn makes the algorithm converge very fast. As well, FASTA-ELM further employ a backward descent step to check objective in each step in order to select the sub-gradient which ensures convergence.

1.7 Thesis Outline

The thesis is structured with 5 main chapters. Chapter 1 introduces the concept of machine learning, which is divided into neural network and extreme learning machine. The chapter also states the problem statement, objectives, and scope of the study. In Chapter 2, in order to point out the advantages and disadvantages of previous techniques. Also, to highlight the techniques that are adopted in this study and the areas the thesis contributes to knowledge, literature review on extreme learning machine by several approaches is

introduced. In chapter 3 the proposed framework on FATSA-ELM and SVM-ELM is presented, and the methodologies utilized are clarified in detail. Chapter 4 presents comprehensive experiment results and discuss on the analysis of findings attained. To conclude, chapter 5 provides the conclusion and recommendation for future studies.

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LIST OF PUBLICATIONS

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