On some specific patterns of  $\tau$ -Adic non-adjacent form expansion over ring Z ( $\tau$ )

## ABSTRACT

Let  $\tau = (-1)^{1-a} + \sqrt{-7/2}$  for  $a \in \{0, 1\}$  is Frobenius map from the set  $E_a(F_2m)$  to it self for a point (x, y) on Koblitz curves  $E_a$ . Let P and Q be two points on this curves.  $\tau$ -adic Non-Adjacent Form (TNAF) of  $\alpha$  an element of the ring  $Z(\tau) = \{\alpha = c+d\tau | c, d \in Z\}$  is an expansion where the digits are generated by successively dividing  $\alpha$  by  $\tau$ , allowing remainders of -1, 0 or 1. The implementation of TNAF as the multiplier of scalar multiplication nP = Q is one of the technique in elliptical curve cryptography. In this study, we find the formulas for TNAF that have specific patterns  $[0, c_1, ..., c_{1-1}]$ ,  $[-1, c_1, ..., c_{1-1}]$ ,  $[1, c_1, ..., c_{1-1}]$  and  $[0, 0, 0, c_3, c_4, ..., c_{1-1}]$ .