UNIVERSITI PUTRA MALAYSIA

SUPPORT VECTOR MACHINE AND ITS APPLICATIONS FOR LINEAR AND NONLINEAR REGRESSION IN THE PRESENCE OF OUTLIERS OF HIGH DIMENSIONAL DATA

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SUPPORT VECTOR MACHINE AND ITS APPLICATIONS FOR LINEAR AND NONLINEAR REGRESSION IN THE PRESENCE OF OUTLIERS OF HIGH DIMENSIONAL DATA

By

WALEED DHHAN SLEABI

Thesis Submitted to the School of Graduated Studies, Universiti Putra Malaysia, in Fulfillment of the Requirements for the Degree of Doctor of Philosophy

September 2016

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DEDICATIONS

- *To the spirit of my father since he passed away when I was at Malaysia 13 March 2013 and I still have remembered his words " my son, do not worry about anything , I pray for you all the time".*

- *To my respectful mother, who has taught me a lot on the meaning of persistency in life.*

- *To my beloved wife for all her contribution, patience and understanding throughout my doctoral studies. She incredibly supported me and made it all possible for me.*

- *To my kids, Mohammed Sadeq, and Hayderali who were accompanying me in all different parts of my study and their love have always been my greatest inspiration.*

Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfillment of the requirements for the degree of Doctor of Philosophy

SUPPORT VECTOR MACHINE AND ITS APPLICATIONS FOR LINEAR AND NONLINEAR REGRESSION IN THE PRESENCE OF OUTLIERS OF HIGH DIMENSIONAL DATA

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September 2016

Chairman : Md. Sohel Rana, PhD
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The ordinary least squares (OLS) is reported as the most commonly used method to estimate the relationship between variables (inputs and output) in the linear regression models because of its optimal properties and ease of calculation. Unfortunately, the OLS estimator is not efficient in cases of the presence of outliers in a data set, nonlinear relationships and high dimensional problems. Thus, the search for alternatives that feature the necessary flexibility to handle them has become an urgent necessity such as nonparametric approaches. Consequently, the support vector regression (SVR) is used as an alternative to OLS.

In this thesis, at first, we consider the identification of outliers through the SVR. In regression, outliers can be classified into two different types, such as vertical outlier and leverage points (good and bad leverage points). It is very important to identify outliers and bad leverage points (BLP) because of their significant effects on estimators. Most of the parametric diagnostic measures are considered good leverage points as bad leverage points. Hence, new nonparametric techniques are proposed for identification outliers that we call the fixed parameters support vector regression methods (FP-SVR). The results of real applications and simulation studies showed that the proposed methods have advantages over classical methods to identify vertical outliers and bad leverage points.

Further, in this thesis, the GM6 version of the robust estimation methods was developed only to identify and inhibit the influence of leverage points (LB) without taking into consideration whether it is good or bad. Thus, a new class of GM-estimators based on FP-SVR technique is developed takes into account minimizing the impact of the bad leverage points only on the model, and we call it GM-SVR. The results show that the performance of the GM-SVR is the best overall, followed by GM6 for all possible combinations of size of samples and percentages of contamination.

This thesis also addresses the problem of high dimensionality in linear and nonlinear regression models. It is well known that the support vector regression has the ability to introduce sparse models (less complexity). Unfortunately, there is a potential problem: if the value of threshold is small (ε near zero), the resulting model depends on a greater number of the training data points, thus making the solution more complexity (non-sparse).Therefore, the single index support vector regression (SI-SVR) model is proposed which combines the flexibility of the nonparametric model and the high accuracy of the parametric model. The real and simulation studies pointed out that the proposed method has the ability to address the problem of high dimensionality.

This thesis also explores the problem of high dimensionality when the number of predictors p larger than the sample size n. Although, we have proposed the SI-SVR to solve the problem of high dimensionality but this model does not have the ability to modeling examples with rank deficient. Furthermore, the efficiency of the resulting SI-SVR model can be decreased and less accurate predictions will be produced when unnecessary predictors are included in the model. Hence, a new method is suggested to overcome this issue using the Elastic Net technique for selecting significant variables which we call the elastic net single index support vector regression (ENSI-SVR). The comparison results show that the ENSI-SVR is an efficient method in dealing with sparse data to achieve dimension reduction which allows applying the SI-SVR easily.

Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia
sebagai memenuhi keperluan untuk ijazah Doktor Falsafah

MESIN VEKTOR SOKONGAN DAN PENGGUNAAN UNTUK REGRESI LINEAR DAN BUKAN LINEAR DENGAN KEHADIRAN TITIK TERPENCIL DAN DATA BERDIMENSI TINGGI

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Kaedah biasa kuasa dua terkecil (OLS) dilaporkan sebagai kaedah yang paling biasa digunakan untuk menganggarkan hubungan antara pembolehubah (input dan output) dalam model regresi linear kerana sifat-sifat yang optimum dan memudahkan dalam pengiraan. Malangnya, penganggar OLS tidak berkesan dalam kehadiran titik terpencil, hubungan tidak linear dan masalah dimensi yang tinggi. Oleh itu, mencari alternatif yang fleksibil telah menjadi satu keperluan yang segera bagi mengendalikan titik terpencil seperti kaedah tidak berparameter. Oleh itu, regresi vektor sokongan (SVR) digunakan sebagai alternatif kepada OLS.

Dalam tesis ini, pada mulanya, kami mengambil kira mengenalpasti titik terpencil melalui SVR . Dalam regresi, titik terpencil boleh diklasifikasikan kepada dua jenis yang berbeza, seperti titik terpencil menegak dan titik tuasan (titik tuasan baik dan buruk). Sangat penting untuk mengenalpasti titik terpencil dan titik tuasan buruk (BLP), ini kerana ianya mempunyai kesan yang signifikan ke atas penganggar. Kebanyakan pengukur diagnostik berparameter mempertimbangkan titik tuasan baik sebagai titik tuasan buruk. Oleh itu, teknik tidak berparameter baru dicadangkan untuk mengenalpasti titik luaran dimana ianya dinamakan Parameter Tetap Menyokong Kaedah Regresi Vektor (FP-SVR). Keputusan bagi aplikasi sebenar dan kajian simulasi menunjukkan kaedah yang dicadangkan mempunyai kebaikan berbanding dengan kaedah yang sedia ada bagi mengenal pasti titik terpencil menegak dan titik tuasan buruk .

Selanjutnya, dalam tesis ini, versi GM6 kaedah anggaran teguh telah dicadangkan hanya untuk mengenalpasti dan menghalang pengaruh titik tuasan tanpa mengambil kira sama ada ianya baik atau buruk. Oleh itu, kaedah baharu penganggar GM berdasarkan parameter tetap menyokong teknik regresi vektor dibangunkan dengan mengambil kira minimumkan kesan daripada titik tuasan buruk hanya kepada model, dan kami menamakannya GM-SVR. Keputusan menunjukkan prestasi GM-SVR adalah yang paling baik untuk keseluruhan, diikuti dengan GM6 untuk kesemua kemungkinan kombinasi saiz sampel dan peratusan data yang tercemar.

Tesis ini juga menangani masalah dimensi tinggi dalam model regresi linear dan tidak linear. Adalah diketahui umum bahawa regresi sokongan vektor mempunyai keupayaan untuk memperkenalkan model jarang (kurang rumit). Malangnya, wujudnya masalah berpotensi: jika nilai ambang adalah kecil (ε hampir sifar), model yang terhasil bergantung kepada bilangan yang lebih besar daripada titik data latihan, dengan itu membuat penyelesaian menjadi lebih kompleks (tidak jarang). Oleh itu, model Tunggal Sokongan Indeks Vektor Regresi (SI-SVR) dicadangkan bagi menggabungkan fleksibiliti model tidak berparameter dan ketepatan yang tinggi bagi model berparameter. Kajian sebenar dan simulasi menunjukkan kaedah yang dicadangkan mempunyai keupayaan untuk menangani masalah dimensi tinggi.

Tesis ini juga meneroka masalah dimensi tinggi apabila bilangan peramal p lebih besar daripada saiz sampel n. Walaupunbagaimanapun, kami mencadangkan SI-SVR untuk menyelesaikan masalah dimensi tinggi tetapi model ini tidak mempunyai keupayaan untuk model contoh dengan susunan kekurangan. Tambahan pula, kecekapan model SI-SVR yang terhasil boleh menurun dan ramalan kurang tepat akan dihasilkan apabila peramal yang tidak perlu dimasukkan dalam model. Oleh itu, satu kaedah baru dicadangkan untuk mengatasi isu ini dengan menggunakan teknik bersih anjal untuk memilih pembolehubah penting yang kami namakan Sokongan Bersih Indeks Tunggal Vektor Regresi Elastik (ENSI-SVR). Keputusan pembandingan mendapati ENSI-SVR merupakan kaedah yang berupaya dalam berurusan dengan data jarang untuk mencapai pengurangan dimensi yang membolehkan penggunaan SI-SVR dengan mudah.

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This thesis was submitted to the Senate of Universiti Putra Malaysia and has been accepted as fulfillment of the requirement for the degree of Doctor of Philosophy. The members of the Supervisory Committee were as follows:

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LIST OF ABBREVIATIONS

BIF	Bounded Influence Function
BLP	Bad Leverage Points
BLUE	Best Linear Unbiased Estimators
BP	Breakdown Point
CDE	Chaos Differential Evolution
DE	Differential Evolution
DOF	Degrees Of Freedom
EGO	Algorithm of Global Optimization
EN	Elastic Net Method
ENSI	Elastic Net Single Index
FP	Fixed Parameters
GM	Generalized M estimators
GS	Grid Search Procedure
HLP	High Leverage Point
IF	Influence Function
iid	Independent Identically Distributed
IRLS	Iteratively Reweighted Least Squares
KKT	Karush Kuhn Tucker Conditions
LASSO	Least Absolute Shrinkage Selection Operator
LAV	Least Absolute Values
LMS	Least Median of Squares
LP	Leverage Point
LTS	Least Trimmed Squares
MAD	Median Absolute Deviation
MCD	Minimum Covariance Determinant
MD	Mahalanobis Distance

MSE	Mean Square Error
MSVR	Modified Support Vector Regression
MVE	Minimum Volume Ellipsoid
NID	Normal Independent Distributed
NNR	Neural Network Regression
OLS	Ordinary Least Squares
OLSC	Ordinary Least Squares for clean data
PCA	Principal Component Analysis
PSO	Particle Swarm Optimization
RBF	Radial Basis Function
RMD	Robust Mahalanobis Distance
SE	Standard Error
SIM	Single Index Model
SLS	Semi-parametric Least Squares
SLT	Statistical Learning Theory
SRM	Structural Risk Minimization
SSVR	Standard Support Vector Regression
SV	Support Vector
SVC	Support Vector Classification
SVM	Support Vector Machine
SVR	Support Vector Regression
VAR	Variance of Residuals
WLS	Weighted Least Squares
WSLS	Weighted Semi-parametric Least Squares

CHAPTER 1

INTRODUCTION

1.1. Introduction and Background of the Study

Regression analysis is a statistical process which aims to explore the functional relationship between two or more variables so that, a dependent variable (output) can be predicted from one or more of independent variables (input) (Kutner et al., 2005). Regression analysis estimates the conditional expectation of the response variable given the explanatory variables. In other words, it estimates the average value of the dependent variable when the independent variables are fixed. This estimation can be done by using the proper technique for the phenomenon or the data set under study such as the ordinary least squares method. The ordinary least squares method (OLS) is classified as one of the prevalent estimation techniques in the regression analysis. Further, the OLS is the most popular estimation method in the linear regression community due to its superior properties and ease of computation, provided that the Gaussian Markov assumptions are met. In addition, the OLS estimator is the best linear unbiased estimator (BLUE), when the random errors are independent identically distributed (iid) normal. Unfortunately, the assumptions of the linear relationship between the variables and the normal distribution of the error term are violated in the most of the real life applications. Furthermore, the OLS estimator is not robust against unusual data points which often appear in real life applications. In other words, the OLS estimator has very low breakdown point which is equal to $1/n$ (Maronna et al., 2006), where n is the sample size. That is, even one point (abnormal) could change the estimate of least squares dramatically in the wrong direction (Rousseeow and Leroy, 1987; Kamruzzaman and Imon, 2002; Maronna et al., 2006).

The assumption of the normal distribution of the error term is violated in the presence of one or more outlier observations. Belsley et al. (1980) reported that the outliers are those points either alone or together with several other points have the largest influence on the computed values of different estimates. Hawkins (1980) defined an outlier observation as the observation that deviates so much from the other observations as to arouse suspicions which it was generated by a various mechanism. Muñoz-Garcia et al. (1990) defined the outlier observation as "An outlier is an observation which being atypical and/or erroneous deviates decidedly from the general behavior of experimental data with respect to the criteria which is to be analyzed on it". Barnett and

Lewis (1994) defined outlier points as those points that are markedly far from the majority of points in a data set. In general, there are several classes of outliers in the regression problems. Observations that are outlying in the Y-direction are expressed as outliers or vertical outliers. In contrast, the observations which are outlying in the X-direction are called high leverage points (HLP). However, there is an urgent need in the regression analysis to find out whether HLP have much impact on the fitting of a model or not (Belsley et al., 1980; Rousseeow and Leroy, 1987).

The other serious problems that affect the predicted model in addition to outliers and the non-linearity relationship among variables are problems of high-dimensional and sparse (p is larger than the number of observations n). The curse of high dimensionality refers to how certain algorithms such as algorithms in numerical analysis, sampling, combinatorics, machine learning and data mining that may perform poorly in high-dimensional data. The common theme of these problems is that when the dimensionality increases, the volume of the space increases so fast that the available data become sparse. This sparsity is problematic for any method that requires statistical significance. In high dimensional data, a matrix related to some algorithms may become singular and some additional information such as regularization, Bayesian prior and others need to be added to obtain standard solution.

Recently, several procedures which deal with these problems separately are available. However, there are not extensive studies reported in the literature which takes into consideration the presence of the non-linearity, outliers and high dimensional problems (full or less than full rank) simultaneously. As a result, the search for alternatives that feature the necessary flexibility to handle these issues has become an urgent necessity such as nonparametric methods especially learning machines.

1.2 Importance and Motivation of the Study

Nonparametric regression technique is a form of statistical regression analysis in which there is no a predetermined form of the predictor but it is constructed based on the information derived directly from the data. Whereas the classical regression statistical techniques stand upon a strict assumption in terms of they assume that the underlying probability distribution of the data is known and the relationship among the variables takes a linear form. However, in real applications, often we confront with distribution-free regression problems with a non-linear relationship between input and output variables (Ukil, 2007). One nonparametric method which is not requiring knowledge of the underlying probability distribution of the data, as well as its ability to deal with non-linear

relationship is the support vector machine. Support vector machine (SVM) is one of the comparatively new and promising techniques for learning separating functions in classification problems (SVC) or for performing function estimation in regression problems (SVR).

Support vector machine was initially applied for classification tasks (Cortes and Vapnik 1995), but shortly, the formulation was extended to deal with regression problems (Smola, and Vapnik 1997; Vapnik 1995). The advantages of support vector machine are its ability to modeling the non-linear relationships by employing kernel trick and its excellent generalization ability on the real applications of the classification and regression problems while it is still capable of producing sparse model (not all observations are needed to find the optimal model) (Ceperic et al. 2014). The common formulation of support vector machine for regression is Vapnik's ε-tube SV regression (ε-SVR) (Smola, and Vapnik 1997). The ε-SVR produces predictive model depends only on a subset of the training points whereas it ignores any points within the threshold ε. This step reveals the potential problem: if the value of threshold ε is small, then the resulting model depends on a greater number of the overall training points, thus making the resulting solution non-sparse, as demonstrated in Guo et al. (2010).

Both of the parametric and nonparametric regression techniques are affected by the presence of single or multiple enormous points in a data (the parametric methods certainly are most influenced than nonparametric methods). Many researchers reported that the real data sets mostly contain unusual points ranging from 1% to 10% (Hampel et al. 1986; Wilcox, 2005). Outliers and HLP have a great effect on the values of various estimates, which leads to misleading conclusions result in wrong decisions. Hence, it is necessary to detect those unusual observations and removing them before embarking on building the predictive model (Cook, 1977) or orientation of the robust methods (Huber, 1973) which minimize the impact of outliers instead of removing them completely from the data. It is worth mentioning that the choose one of these methods is up to the researcher.

There are several parametric methods used for detecting single or multiple outliers and HLP. Unfortunately, they are not successful to identify multiple abnormal points in the data sets due to the effects of masking and swamping problems (Rousseeuw and Leroy, 1987). On the other hand, these methods can not deal with less than full rank data. To address this problem some researchers explored the use of non-parametric methods for outlier detection in cases both of full rank and less than full rank. Jordaan and Smits (2004) suggested using standard support vector regression (SSVR) for outlier detection. The idea of this technique is by running the SV regression model

many times and detects points which are suspected as outliers. Nishiguchi et al. (2010) pointed out that some problems arise when applying it with real applications. It requires high computational costs for multiple outliers in the data because detection of an outlier requires a number of iterations of the calculation; the trial and error is used for accurate detection, since it is not clear how to identify the outlier threshold value. To remedy this problem, Nishiguchi et al. (2010) developed the modified support vector regression (MSVR) technique for outlier detection by employing new trade-off parameter (μ), which is successful in identifying outliers and HLP. Nonetheless, the MSVR approach is suitable for few outliers in the data, since one iteration is required to detect one outlier. Consequently, computational costs become close to those arising from the standard SVM regression method in case of presence multiple outliers. Further, there is no clear rule for choosing the value of threshold parameter, although it comes with fixed value of this parameter. The shortcoming of these methods has inspired us to develop new techniques to improve the performance of standard SVM regression for outlier detection, which we call the fixed parameters support vector regression (FP-SVR). The proposed two methods are expected to achieve accurate detection of outliers and HLP (only bad leverage points) with fixed parameters during one iteration.

This thesis also concerned on the use of robust methods to address the problem of the presence of outliers and bad leverage points (BLP) in multiple linear regression models. As we mentioned previously the OLS estimator is seriously affected by the presence of outliers. One of the most common alternative techniques to OLS of addressing the presence of outliers is the robust regression procedure (Hampel, 1974). There are many robust regression methods in the literature, such as the least absolute values (LAV), the M-estimator, generalized M-estimator (GM1-estimator), the least median of squares (LMS), the S estimator, the least trimmed squares (LTS), the MM estimator and new class of GM-estimator (GM6) proposed by Coakley and Hettmansperger (1993). Yohai and Zamar (1988) firmly recommended that one of the goals of robust regression technique is to achieve: (a) a high breakdown point of nearly 50%, (b) a bounded influence function and (c) a high efficiency, simultaneously. According to this recommendation, only GM6 method achieves the three conditions, (a), (b) and (c) simultaneously. Regrettably, this method considers the good leverage points to be bad leverage points, which means that its efficiency tends to decrease with the presence of "good" leverage points. This limitation has inspired us to develop a new class of GM-estimators based on a fixed parameters support vector regression techniques that have been proven in Chapter 3, takes into account minimizing the impact of the bad leverage points only on the model, and we call it GM-SVR.

This thesis also addresses the problem of high dimensionality in linear and nonlinear regression models. It should be noted that the sparsity feature (less complexity), which is characterized by the SVR model by itself is not sufficient to ensure good generalization to the model in addition to the problem of non-sparse that accompany the small threshold, ε near zero (Ceperic et al. 2014). It is well known the support vector regression is a fully nonparametric approach, which makes it a flexible but at the same time it is suffering from precision decrease when increasing the covariates which is called the curse of the high-dimensionality (Härdle et al. 2004). For this reason, the alternative is used to cope with this drawback. One of the common techniques to improve generalization accuracy and overcome the curse of the high dimensional problem is the single index model. Ichimura (1993) suggested a semi-parametric model which combines between the flexibility of the nonparametric model and the high accuracy of the parametric model called single index model. This model summarizes the covariates within a single variable called index. To the best of our knowledge, there is no existing research in literature which used SVR to evaluate the unknown link function of the single index model. This inspires us to propose a new technique that uses the SVR model to estimate the unknown link function of the single index model namely the single index support vector regression (SI-SVR).

It should be stated that the SI-SVR model does not have the ability to modeling the rank deficient data. Furthermore, the efficiency of the resulting model could be declined, and less accurate predictions will be produced when unnecessary predictors are included in the model (Tibshirani, 1996; Hastie et al., 2009). This requires development of a new method to overcome this issue. This can be done by employing the concept of variables selection to achieve the possibility of modeling by single index model which we call the elastic net single index support vector regression (ENSI-SVR).

1.3 Research Objectives

The main goal of this thesis is to investigate the high dimensionality problems for linear and nonlinear regression models in the presence of outliers (outlying in coordinates X and Y). The classical estimation methods such as the ordinary least squares (OLS) method are not robust against outliers. Moreover, they can not evaluate the nonlinear relationships and the difficulty to meet all the assumptions for high-dimensional data. The foremost objectives of our research can be outlined systematically as follows:

1. To propose new improved diagnostic methods for the identification of multiple outliers based on two types of kernel functions.

2. To formulate a new robust estimation method to remedy the presence of outliers in the data for the linear regression model.
3. To propose a new semi-parametric method to cope the curse of high dimensionality combines between the high precision of parametric methods and the flexibility of nonparametric methods.
4. To develop the elastic net penalty approach for selecting variables in a single index support vector regression model to overcome the curse of high dimensionality when the number of predictors, p is larger than sample size n.

1.4 Scope and Limitation of the Study

The linear and nonlinear regression models are widely used in many areas of studies such as bioinformatics, economics, financial predictions and social sciences. In the real situation, these regression models have many practical uses. However, the most applications of the linear regression models are evaluated using the OLS method because of the ease of computation and its optimal properties when the underlying assumptions are met. In reality, the OLS estimator is not resistant to outlying samples; even one outlier can destroy the OLS estimator. The alternative procedures which used to address this issue are detection methods and robust statistical methods. Flexible techniques are suggested to the identification of outliers and HLP such as SSVR and MSVR in cases of full and less than full rank data. Nonetheless, these existing methods basically focus only on the identification of leverage points without taking into consideration their classification into good and bad leverage points. It is very important to detect and classify the good and bad leverage points, as only bad leverage points are responsible for the misleading conclusion about the fitting of the regression model. On the other hand, many robust statistical estimation techniques are suggested such as LMS-estimator, LTS-estimator, M-estimator, GM1-estimator, MM-estimator, and GM6-estimator. However, some of these methods are not robust against leverage points and some methods are considered the good leverage points as bad leverage points.

The other technique of statistical modeling is the nonparametric procedure which used to evaluate the nonlinear relationships and high dimensional problems including when the number of predictors p much greater than sample size n. One of the most effective methods in the nonparametric machine learning community is the support vector machine (Frohlich and Zell, 2005). However, the ability of the SVM model to evaluate the high dimensional problems is decreased because of the resulting model is non-sparse when the threshold is small. Furthermore, the generalization performance of SVM depends heavily on the right selection of the hyper-parameters C and ε, so the

major issue for practitioners attempting to apply SVM is how to set these parameter values to guarantee a good generalization performance for a training data set. It should be noted all calculations have been implemented using R software.

1.5 Overview of the Thesis

In accordance with the objectives and the scope of the study, the contents of this thesis are structured in the eight chapters. The thesis chapters are organized so that the study objectives are apparent and are conducted in the sequence outlined.

Chapter Two: This chapter briefly presents the literature review of the least squares estimation method and the violations of its underlying assumptions such as the departure of normality and the presence of outliers. The literature review of the support vector machine for regression and its basic idea to employ the kernel trick during the estimation process are highlighted. The outliers, and leverage points and their diagnostics methods are also discussed. Moreover, basic concepts of robust linear regression and some important existing robust regression methods are also reviewed. Bootstrapping methods are also briefly discussed. In this chapter, the main idea of the single index model and its estimation methods are also discussed. Finally, the concept of variable selection and some of penalization methods are also briefly highlighted.

Chapter Three: This chapter discusses the existing SSVR and MSVR which are developed by Jordaan and Smits (2004) and Nishiguchi et al. (2010). The new proposed methods (FP-SVR) for the identification of multiple vertical outliers and bad leverage points are presented in this chapter. The steps for proposed FP-SVR methods and its algorithm are also highlighted. Finally, some real and simulation studies are discussed to evaluate the performance of the proposed methods.

Chapter Four: This chapter deals with the development of the GM-estimator based on FP-SVR (denoted by GM-SVR) for data having outliers and bad leverage points. Two Monte Carlo simulation studies and two numerical examples are carried out to assess the performance of the proposed method.

Chapter Five: In this chapter, we present the proposed semi-parametric model to address the high dimensional problem, namely the single-index support vector regression (denoted by SI-SVR).The new proposed technique is useful to get rid the so-called the curse of high dimensionality. In this respect, two types

of data are considered, the linear and nonlinear relationships. The numerical and simulation examples are also discussed to assess our proposed method.

Chapter Six: In this chapter, the concept of variable selection is utilized to achieve non-singular predictive matrix when the number of predictors p larger than sample size n. Then, the proposed model, namely the elastic net single-index support vector regression (denoted by ENSI-SVR) can be used to remedy the curse of high dimensionality. The semi-parametric proposed model combines the high accuracy of parametric methods and the flexibility of nonparametric methods. A Monte Carlo simulation studies and numerical example are given to assess the performance of the proposed method.

Chapter Seven: This chapter provides the summary and detailed discussions of the thesis conclusions. Areas for future research are also recommended.

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