

A general relation between sums of cubes and triangular pyramidal numbers

ABSTRACT

Let $c_k(m)$ denote the number of representations of integer m as a sum of k cubes and $p_k(m)$ denote the number of representations of integer m as a sum of k triangular pyramidal numbers. We give a relation $p_k(m) = c_{k+1}(m)$ where $m = 48n + 24n + 2\tilde{n} + k$ and $c_{k+1}(m)$ denotes the number of representations of integer m as a sum of $k+1$ odd cubes, for a single value of m . A general relation between number of representations between $\sum_{k=1}^s x_k$ and its associated polytopic numbers for any orders of s , is also given.

Keyword: Number of representations; Sum of cubes; Sum of triangular pyramidal numbers