Description of the first disc $\Delta_1(t)$ of the commuting graph C(G, X) for elements of order three in symmetric groups

ABSTRACT

The commuting graph C(G, X), where G is a finite group and X is a subset of G, is the graph whose vertex set is X and two distinct elements of X being joined by an edge whenever they commute in the group G. Here the CG(t)-orbit representatives and the number of elements in the first disc $\Delta_1(t)$ of C(G, X), is studied when G is a symmetric group of degree n, Sym(n) and X is a conjugacy class of elements of order three.

Keyword: Commuting graph C(G, X); $\Delta_1(t)$; Symmetric group; Order three