



UNIVERSITI PUTRA MALAYSIA

**HYBRID METAHEURISTIC ALGORITHM AND METAHEURISTIC
PERFORMANCE MEASUREMENT FOR SOLVING UNIVERSITY
COURSE TIMETABLING PROBLEM**

ABU BAKAR MD SULTAN

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TIMETABLING PROBLEM**

By

ABU BAKAR MD SULTAN

**Thesis Submitted to School of Graduate Studies, Universiti Putra Malaysia in
Fulfilment of the Requirement for the Degree of Doctor of Philosophy**

August 2007



DEDICATION

*This thesis is dedicated to my parents, my wife and to anyone who thought me more about
forbearance, fortitude and forgiveness*



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfilment
of the requirement for the degree of Doctor of Philosophy

**HYBRID METAHEURISTIC ALGORITHM AND
METAHEURISTIC PERFORMANCE MEASUREMENT FOR
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Chairman: Associate Professor Ramlan Mahmud, PhD

Faculty: Computer Science and Information Technology

Metaheuristics have received considerable interest in the fields of applied artificial intelligence and combinatorial optimization such as university course timetabling problem (UCTP). Metaheuristics begin with one or more initial solutions and iteratively employ search strategies to avoid local optima.

Recently, it was observed that the combination of concepts of different metaheuristics, called hybrid metaheuristics, can provide a more efficient behavior and higher flexibility in dealing with real-world and large-scale problems. Frequently, hybridizing the metaheuristic components lie on how we can effectively structure metaheuristic components to efficiently explore



and exploit search space. Acquiring the proper balance between intensification and diversification strategies is the crucial factor in obtaining an effective metaheuristic. This research focused on the implementation of an hybrid evolutionary metaheuristic namely Two_point Hybrid Evolutionary Algorithm (Tp_HEA) on university course timetabling problem instances (UCTP). Tp_HEA is based on two solutions that represent intensification at one point and diversification on the other point. Systematic exchange of information between these two points is to ensure the proper management of the balance between intensification and diversification.

The proposed Tp_HEA was tested on twelve standard UCTP instances according to the specified experimental procedure. The result obtained from the average point analysis and percentage of invalid solution was very promising. Out of twelve datasets, eight produced better performance when comparison was made against five other metaheuristics. The performance was measured in terms of constraints solved. Experimental results revealed that the arrangement of the Tp_HEA component would affect the search landscape of most UCTP problem instances.

The stochastic nature of metaheuristic including the Tp_HEA, results in inconsistent performance and the difficulty in obtaining accurate prediction from average point analyses. Thus, the second contribution of this research



is the introduction of Metaheuristic Performance Measurement (MPM). MPM is the attempt of measuring metaheuristic performance statistically, thus accurate indices can be obtained.

The validity of MPM as a new measuring technique was tested using selected results obtained from proposed Tp_HEA together with the result produced by genetic algorithm (GA). The analysis showed that MPM values obtained from both algorithms almost in line with the result obtained from average point analysis. The specific indices of performance produced by MPM were the major elements that differentiate MPM from average point analysis. The indices gave values for the performance, and thus the performance was more easily estimated. The reliability of MPM could be further observed when the analysis of variance showed that MPM values obtained from different independent runs were not significantly varied. Therefore, MPM was able to obtain a good estimation as compared to other commonly used metaheuristic measuring techniques.



Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia
sebagai memenuhi keperluan untuk ijazah Doktor Falsafah

**ALGORITMA METAHEURISTIK HIBRID DAN PENGUKUR
PRESTASI METAHEURISTIK UNTUK PENYELESAIAN
MASALAH PENJADUALAN KURSUS UNIVERSITI**

Oleh

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Pengerusi: Profesor Madya Ramlan Mahmod, PhD

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Metaheuristik telah menarik banyak perhatian dalam bidang aplikasi kecerdasan buatan dan pengoptimuman kombinatorial seperti masalah penjadualan kursus universiti. Kaedah metaheuristik bermula dengan satu atau lebih penyelesaian awal dan secara lelaran menggunakan strategi-strategi carian untuk menghindar berlakunya optima awal.

Terbaru, didapati penggabungan konsep dari metaheuristik yang berbeza dipanggil penghibridan metaheuristik boleh menghasilkan gelagat yang efisien dan fleksibel dalam menyelesaikan masalah sebenar dan besar. Selalunya penghibridan metaheuristik terletak kepada bagaimana kita boleh menstrukturkan secara efektif komponen-komponen metaheuristik supaya



penjelajahan dan penyusupan ruang carian berlaku dengan efisien. Mendapatkan imbangan yang bersesuaian antara intensifikasi dan diversifikasi adalah isu penting menghasilkan metaheuristik yang efektif. Penyelidikan ini memfokus kepada pelaksanaan metaheuristik lelaran hybrid yang dinamakan Algoritma Hibrid Dua Titik Metaheuristik (Tp_HEA) ke atas masalah penjadualan kursus universiti (UCTP). Tp_HEA berasaskan kepada dua penyelesaian yang mewakili intensifikasi di satu titik dan diversifikasi di satu titik lain. Pertukaran maklumat bersistematik antara dua titik ini untuk memastikan imbangan antara intensifikasi dan diversifikasi diurus sebaiknya.

Tp_HEA yang diperkenalkan diuji ke atas duabelas UCTP piawai menuruti prosedur pengujian dinyatakan. Keputusan yang diperolehi dari analisa purata dan peratusan penyelesaian yang tidak sah amat menggalakkan. Dari duabelas dataset, lapan menghasilkan prestasi lebih baik bila perbandingan dibuat dengan lima metaheuristik yang lain. Proses-proses pengujian yang mendalam mendapati pengstrukturkan komponen-komponen yang berbeza-beza memberi kesan ke atas landskap carian masalah UCTP dibawah kajian. komponen yang berbeza memberikan kesan ke atas landskap carian kepada semua masalah UCTP yang dikaji.

Ciri stokastik metaheuristik menjadikan ianya sukar diukur dari segi prestasi. Dengan itu sumbangan kedua kajian ini adalah pengenalan kepada



Pengukuran Prestasi Metaheuristik (MPM). MPM merupakan pendekatan mengukur prestasi metaheuristik melalui kaedah statistik bagi membolehkan indek tepat diperolehi.

Kebolehan MPM sebagai teknik pengukur baru diuji menggunakan keputusan terpilih yang diperolehi dari Tp_HEA bersama keputusan yang dihasilkan oleh algoritma genetic (GA). Analisa menunjukkan nilai-nilai MPM yang diperolehi dari kedua-dua algoritma adalah selari dengan yang didapati dari analisa purata, hanya MPM memberikan index sebagai penunjuk kepada prestasi. Kebolehpercayaan MPM selanjutnya boleh dilihat dari analisa varian yang menunjukkan nilai-nilai MPM yang diperolehi dari larian berasingan tidak begitu berbeza. Oleh itu MPM berkebolehan mendapatkan anggaran yang baik jika dibandingkan dengan lain-lain teknik pengukuran metaheuristik yang biasa digunakan.



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I certify that an Examination Committee has met on 13th August 2007 to conduct the final examination of Abu Bakar Md Sultan on his Doctor of Philosophy thesis entitled "Two Point Hybrid Metaheuristic and Metaheuristic Performance Measurement for University Course Timetabling Problem" in accordance with Universiti Pertanian Malaysia (Higher Degree) Act 1980 and Universiti Pertanian Malaysia (Higher Degree) Regulations 1981. The Committee recommends that the candidate be awarded the relevant degree. Members of the Examination Committee are as follows:

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DECLARATION

I hereby declare that the thesis is based on my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously or concurrently submitted for any other degree at UPM or other institutions.

ABU BAKAR BIN MD SULTAN

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LIST OF ABBREVIATIONS

ACO	Ants Colony Optimization
AI	Artificial Intelligence
ANOVA	Analysis of Variance
COP	Combinatorial Optimization Problem
CRD	Completely Randomized Design
EA	Evolutionary Algorithms
FDC	Fitness Distance Correlation
GA	Genetic Algorithm
GLS	Guided Local Search
GRASP	Greedy Randomized Adaptive Search Procedure
ILS	Iterated Local Search
MA	Memetic Algorithm
MN	Metaheuristic Network
MPM	Metaheuristic Performance Measurement
NP	Nondeterministic Polynomial
PATAT	Practice and Theory of Automated Timetabling
SA	Simulated Annealing
TS	Tabu Search
TSP	Traveling Salesman Problem
Tp_HEA	Two_point Hybrid Evolutionary Algorithm
UCTP	University Course Timetabling Problem
QAP	Quadratic Application Problem





CHAPTER 1

INTRODUCTION

1.1 Background to the Research

Timetabling problems have attracted the continuous interest of researchers mainly because the problems provide the opportunity of testing combinatorial solution methods in formulations that represent difficult practical problems (Dimopoulou and Miliotois, 2001). Reis and Oliviera (2001) and He *et al.* (2005) reported that scientific community has given considerable amount of attention to automated timetabling during the last four decades according to the variants of timetabling literature published since then.

Timetable scheduling is an activity of assigning subjects to time and space such that all constraints are satisfied (Deris *et al.*, 2000). It can be categorized into several types and the most common type is academic university, college and school timetabling. The problem of constructing course timetables for higher learning institutions consist of allocating the set of courses offered by a university to a time period and classrooms in such a way that no teacher, student or room is used more than once at a specific time.

