

UNIVERSITI PUTRA MALAYSIA

OPTICAL AND THERMAL CHARACTERIZATION OF ZINC OXIDE-BASED CERAMIC USING PYROELECTRIC AND PHOTOPYROELECTRIC TECHNIQUES

SABRINA MOHD SHAPEE

FS 2009 1



OPTICAL AND THERMAL CHARACTERIZATION OF ZINC OXIDE-BASED CERAMIC USING PYROELECTRIC AND PHOTOPYROELECTRIC TECHNIQUES

By

SABRINA MOHD SHAPEE

Thesis Submitted to the School of Graduate Studies, Universiti Putra Malaysia, in Fulfillment of the Requirements for the Degree of Master of Science

October 2008



DEDICATION

To my beloved parents Mohd Shapee Shamsudin and Nasriah Mansor For their love and care...

To my husband Mohd Rafizu Muda Whose make me feel that I am perfect...

To my sister Herdayu and my brothers Mohd Safuan, Mohd Hafiz and Mohd Syukri For making my life complete...

To all my very wonderful friends For making my life full of joy and happiness...

To all my lecturers For helping me a lot throughout my study...

To me May Allah bless me always...



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfillment of the requirement for the degree of Master of Science

OPTICAL AND THERMAL CHARACTERIZATION OF ZINC OXIDE-BASED CERAMIC USING PYROELECTRIC AND PHOTOPYROELECTRIC TECHNIQUES

By

SABRINA MOHD SHAPEE

October 2008

Chairman : Azmi Zakaria, Ph.D.

Faculty : Science

The advantage of wide electrical band-gap of zinc oxide (ZnO) semiconductor has been used in many applications particularly as varistors, which are ceramic devices with highly non-linear current-voltage characteristics. For ZnO-based varistor system, one or more additive oxides such as antimony oxide (Sb₂O₃), bismuth oxide (Bi₂O₃) and cobalt oxide (Co₃O₄) are the main tools that improve the nonlinear response and the stability of ZnO varistor.

The thermal and optical characteristics of ZnO-based ceramic have been carried out at room temperature using pyroelectric and photopyroelectric techniques, respectively, that use polyvinylidene fluoride film as detector. In thermally thick regime, the thermal diffusivity value is obtained from the plot of the product of modulation frequency (f)



times pyroelectric amplitude signal versus \sqrt{f} . The thermal diffusivity obtained for pure ZnO ceramic sample without potassium bromide (KBr) (0.079 cm²s⁻¹) close to literature values, indicates the reliability of the present set up. The thermal diffusivity of doped ZnO ceramic in KBr matrix was prepared by mixing the ground ceramic with KBr and pressed into a pellet form. Before the sample was attached to the pyroelectric detector it was covered with carbon soot to turn it into an optically opaque condition. It is observed that the thermal diffusivity of ceramic ZnO doped with Bi₂O₃ in the KBr matrix increases with the increase of Bi₂O₃ mol percentage.

The photopyroelectric spectrometer has been used to obtain optical absorption spectrum of ZnO based ceramic doped with various mol percentages of Bi₂O₃, Co₃O₄ and Sb₂O₃. The photopyroelectric optical spectra of thin layer of ceramic samples, put directly on photopyroelectric detector, were used to determine the band-gap energy of the samples. The results indicate that for all dopants the band-gap energy of ZnO decreases with the increase of dopant mol percentage. Microstructural characterization has been made on the ZnO-based ceramic by addition of different metal oxides. All of the samples were characterized using scanning electron microscopy (SEM) and X-ray diffraction (XRD).

Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia sebagai memenuhi keperluan untuk ijazah Master Sains.

PENCIRIAN OPTIK DAN TERMA BAGI SERAMIK BERASASKAN-ZINK OKSIDA MENGGUNAKAN TEKNIK PIROELEKTRIK DAN FOTOPIROELEKTRIK

Oleh

SABRINA MOHD SHAPEE

Oktober 2008

Pengerusi : Azmi Zakaria, Ph.D.

Fakulti : Sains

Kelebihan semikonduktor zink oksida (ZnO) yang mempunyai nilai jurang-jalur elektrik lebar telah digunakan dalam pelbagai aplikasi khususnya sebagai varistor, yang mana ia adalah peranti seramik yang mempunyai ciri-ciri arus-voltan tak-linear yang tinggi. Bagi sistem varistor berasaskan ZnO, satu atau lebih campuran oksida seperti antimoni oksida (Sb₂O₃), bismuth oksida (Bi₂O₃) dan kobalt oksida (Co₃O₄) adalah bahan utama yang digunakan untuk meningkatkan respons tak-linear dan kestabilan varistor ZnO.

Pencirian optik dan terma seramik berasaskan ZnO telah dijalankan pada suhu bilik menggunakan teknik piroelektrik dan fotopiroelektrik masing-masingnya, menggunakan filem polyvinylidene fluoride sebagai pengesan. Di dalam keadaan ketebalan secara terma, nilai keresapan terma diperolehi melalui kelok hasil-darab frekuensi modulasi (f)



dengan isyarat amplitud piroelektrik melawan \sqrt{f} . Keresapan terma diperolehi bagi sampel seramik ZnO tulen tanpa potasium bromida (KBr) (0.079 cm²s⁻¹) menghampiri nilai literatur menunjukkan kejituan radas tersedia. Keresapan terma bagi seramik ZnO yang telah didopkan bersama-sama matriks KBr disediakan dengan mencampurkan seramik yang telah ditumbuk halus bersama-sama KBr dan dihasilkan menjadi bentuk pelet. Sebelum sampel dilekatkan kepada pengesan piroelektrik, ia disalut dengan jelaga untuk menjadikannya berkeadaan legap optik. Didapati bahawa keresapan terma seramik ZnO didopkan dengan Bi₂O₃ di dalam matriks KBr meningkat dengan peningkatan peratus mol Bi₂O₃.

Spektrometer fotopiroelektrik telah digunakan untuk mendapatkan spektrum penyerapan optik bagi ZnO berasaskan seramik didopkan secara berasingan dengan pelbagai peratus mol Bi₂O₃, Co₃O₄ dan Sb₂O₃. Spektra optik fotopiroelektrik bagi lapisan nipis sampel seramik, diletakkan secara terus di atas pengesan fotopiroelektrik, digunakan untuk menentukan tenaga jurang-jalur bagi sampel. Keputusan menunjukkan bagi kesemua pendopan, tenaga jurang-jalur bagi ZnO berkurang dengan penambahan peratus mol pendopan. Pencirian mikrostruktur juga telah dijalankan bagi seramik berasaskan ZnO dengan penambahan pelbagai bahan metal oksida. Kesemua sampel telah dicirikan menggunakan mikroskopi elektron imbaan (SEM) dan pembelauan sinar-X (XRD).



ACKNOWLEDGEMENTS

First and foremost I would like to express my deepest praise to Allah that has given me the strength, faith, confidence and patience to complete this project within the required time frame despite all the challenges. I am very grateful to my supervisor Assoc. Prof. Dr. Azmi Zakaria, who invited me in his research group, taught me, guided and encouraged me along the way. I would also like to acknowledge all my co-supervisors, Assoc. Prof. Dr. Mansor Hashim, Prof. Dr. W. Mahmood Mat Yunus and Prof. Dr. Abdul Halim Shaari for their advices and helpful discussions during this period of study.

Special thanks are also given to Assoc. Prof. Dr. Zaidan Abdul Wahab and Dr. Zainul Abidin Hassan for fruitful discussions. My appreciation also goes to all staffs in the Department of Physics for their assistance and co-operation throughout my study. I must also thank Mrs. Rusnani Amiruddin from FT-IR Laboratory and also Assoc. Prof. Dr. Fauziah Othman and all staffs from Microscopy and Microanalysis Unit, for helping me in handling the Scanning Electron Microscope (SEM). I am very grateful for the PASCA scholarship awarded by the Universiti Putra Malaysia, which enabled me to undertake this work.

My sincere thanks to all my wonderful friends and my seniors especially Liaw Hock Sang and Kak Rosidah Alias for abundantly assisted me in my research and also who involved directly or indirectly towards the success of this project. Last but not least, a very deepest gratitude for my family for their patience and encouragement during my postgraduate study.



I certify that a Thesis Examination Committee has met on 16 October 2008 to conduct the final examination of Sabrina binti Mohd Shapee on her thesis entitled "Optical and Thermal Characterization of Zinc Oxide-Based Ceramic Using Pyroelectric and Photopyroelectric Techniques" in accordance with the Universities and University College Act 1971 and the Constitution of the Universiti Putra Malaysia [P.U.(A) 106] 15 March 1998. The Committee recommends that the student be awarded the Master of Science.

Members of the Thesis Examination Committee were as follows:

Mohd Maarof H. A. Moksin, PhD Professor Faculty of Science Universiti Putra Malaysia (Chairman)

Zainal Abidin Sulaiman, PhD

Associate Professor Faculty of Science Universiti Putra Malaysia (Internal Examiner)

Zulkifly Abbas, PhD

Senior Lecturer Faculty of Science Universiti Putra Malaysia (Internal Examiner)

Senin Hassan, PhD

Professor Faculty of Science and Technology Universiti Malaysia Terengganu (External Examiner)

HASANAH MOHD. GHAZALI, PhD

Professor and Dean School of Graduate Studies Universiti Putra Malaysia

Date: 29 January 2009



This thesis submitted to the Senate of Universiti Putra Malaysia and has been accepted as fulfillment of the requirement for the degree of **Master of Science**. The members of the Supervisory Committee were as follows:

Azmi Zakaria, PhD

Associate Professor Faculty of Science Universiti Putra Malaysia (Chairman)

Mansor Hashim, PhD

Associate Professor Faculty of Science Universiti Putra Malaysia (Member)

Abdul Halim Shaari, PhD

Professor Faculty of Science Universiti Putra Malaysia (Member)

Wan Mahmood Mat Yunus, PhD

Professor Faculty of Science Universiti Putra Malaysia (Member)

HASANAH MOHD. GHAZALI, PhD

Professor and Dean School of Graduate Studies Universiti Putra Malaysia

Date: 12 February 2009



DECLARATION

I declare that the thesis is my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously, and is not concurrently, submitted for any other degree at Universiti Putra Malaysia or at any other institution.

SABRINA MOHD SHAPEE

Date:



TABLE OF CONTENTS

DEDICATION	ii
ABSTRACT	iii
ABSTRAK	v
ACKNOWLEDGEMENTS	vii
APPROVAL	viii
DECLARATION	х
LIST OF TABLES	xiii
LIST OF FIGURES	xiv
LIST OF ABBREVIATIONS	xvi
LIST OF SYMBOLS	xviii

CHAPTER

1	INTRODUCTION			
	1.1	Introduction	1	
	1.2	Motivation and Problem Statement	1	
	1.3	Objectives	3	
2	LITI	ERATURE REVIEW		
	2.1	Introduction	4	
	2.2	Review on Thermal Diffusivity of ZnO-Based Ceramic	5	
	2.3	Photopyroelectric Spectroscopy	8	
	2.4	Photopyroelectric Spectra of ZnO Based Ceramic	12	
	2.5	Zinc Oxide Varistor	14	
3	THE	CORY		
	3.1	Introduction	16	
	3.2	Photothermal Spectroscopy	17	
	3.3	Photopyroelectric Detection	20	
	3.4	Photopyroelectric Effect	21	
		3.4.1 One-Dimensional Model of Photopyroelectric Theory	23	
		3.4.2 Optically Opaque and Thermally Thick Pyroelectric	25	
	3.5	Thermal Diffusivity	28	
	3.6	Photopyroelectric Measurements of Thermal Diffusivity	29	
	3.7	Theory on Zinc Oxide	30	
	3.8	Optical Band-Gap Energy	33	
		3.8.1 Band-Gap Energy in ZnO	34	





		3.8.2 Band-Gap Energy of Semiconductors	36
	3.9	Microstructure of ZnO	37
	3.10	Zinc Oxide Varistor	39
	3.11	Effect of Additives	42
4	MET	HODOLOGY	
	4.1	Introduction	44
	4.2	Sample Detection Scheme	44
	4.3	Thermal Diffusivity Measurement System	45
	4.4	Spectrometer System	47
	4.5	Sample Preparation of ZnO-Based Ceramic	50
	4.6	Microstructural Observation	56
5	RESU	ULTS AND DICUSSION	
	5.1	Introduction	58
	5.2	Thermal Diffusivity Measurements by Pyroelectric Method	58
		5.2.1 ZnO Doped With Bismuth Oxide	63
	5.3	Optical Band Gap Energy Analysis	65
		5.3.1 ZnO Doped With Bismuth Oxide	66
		5.3.2 ZnO Doped With Cobalt Oxide	71
		5.3.3 ZnO Doped With Antimony Oxide	76
6	CON	CLUSION AND RECOMMENDATION FOR FUTURE	
	RESI	EARCH	
	6.1	Introduction	81
	6.2	Conclusions	81
	6.2	Recommendation for Future Research	83
RE	FEREN	ICES	84
API	PENDI	CES	89
BIC	BIODATA OF THE STUDENT 93		
LIS	T OF F	PUBLICATIONS	94





LIST OF TABLES

Table		Page
3.1	Role of additives in ZnO Varistors	43
5.1	The comparison of present thermal diffusivity values to the literature values.	62
5.2	Thermal diffusivity ZnO-Bi ₂ O ₃ in KBr matrix	63
5.3	Band-gap energy of ZnO doped with Bi_2O_3 at different mol %	70
5.4	Band-gap energy of ZnO doped with Co_3O_4 at different mol%	74
5.5	Band-gap energy of ZnO doped with Sb ₂ O ₃ at different mol %	79



LIST OF FIGURES

Figures		Page
2.1	Most commonly used photopyroelectric (PPE) configurations: (a) Standard (SPPE), (b) Inverse (IPPE), (c) Non-Contact-Back-(NC-BPPE) and (d) Non-Contact-Front- (NC-FPPE) configuration.	6
3.1	PT phenomena caused by illumination of a surface by modulated beam of light (Almond and Patel, 1996).	19
3.2	One dimensional geometry of the photopyroelectric system	22
3.3	Wurzite structure of ZnO	31
3.4	Energy bands of ZnO	32
3.5	Energy bands in Solids	35
3.6	Energy band diagram proposed by Blatter and Greuter. Double Schottky barriers are formed by interface states and traps. The breakdown is caused by hole accumulation at the grain boundary. The holes are generated by impact ionization in the depletion region.	35
3.7	Development of the grain boundaries during sintering	38
3.8	(a) Current (I)-voltage (V) curve of a typical ZnO varistor. (b) Schematic I-V curves for different non-Ohmic exponents, γ	39
3.9	Proposed electronic structure at a junction between ZnO grains: (a) no voltage applied; (b) with applied voltage. (Moulson et al, 1990)	41
4.1	Schematic diagram of PPE cell	45
4.2	Thermal diffusivity measurement set-up using PVDF film sensor	46
4.3	Photopyroelectric spectrometer system	47
4.4	PPE spectrum of carbon black	50
4.5	Flowchart of sample preparation	51
5.1	Plot of PE signal versus frequency of Al sample of thickness 0.0486cm.	59
5.2	Plot of ln (<i>f</i> <i>V</i>) versus \sqrt{f} of Al sample of thickness 0.0486 cm.	60



5.3	Plot of ln $(f V)$ versus \sqrt{f} of pure KBr sample of thickness 0.0540mm.	60
5.4	Plot of ln ($f V $) versus \sqrt{f} of pure ZnO sample of thickness 0.0670 cm.	61
5.5	Increasing of thermal diffusivity value of mixture KBr with 1 wt% $ZnO-Bi_2O_3$.	64
5.6	$(\rho hv)^2$ versus photon energy for pure ZnO	66
5.7	The XRD patterns for samples pure ZnO and ZnO- Bi_2O_3	67
5.8	SEM microstructure for ZnO Doped With Bismuth Oxide	68
5.9	Normalised PPE spectra of ZnO and ZnO-Bi ₂ O ₃ .	69
5.10	$(\rho h v)^2$ versus photon energy for ZnO doped with 3-mol% Bi ₂ O ₃	69
5.11	Bi_2O_3 content dependence of energy band-gap of the ZnO	70
5.12	The XRD patterns for samples pure ZnO and ZnO doped with 1.8-mol% $\mathrm{Co}_3\mathrm{O}_4.$	72
5.13	SEM microstructure for ZnO Doped with Cobalt Oxide	72
5.14	Normalised PPE spectra of ZnO doped with Co ₃ O ₄	73
5.15	$(\rho h v)^2$ versus photon energy for ZnO doped with 0.6-mol% Co ₃ O ₄	73
5.16	Co_3O_4 content dependence of energy band-gap energy of the ZnO	75
5.17	The XRD patterns for pure ZnO and ZnO-Sb ₂ O ₃	77
5.18	SEM microstructure for ZnO Doped with Antimony Oxide	77
5.19	Normalised PPE spectra of ZnO and ZnO-Sb ₂ O ₃	78
5.20	$(\rho h v)^2$ versus photon energy for ZnO doped with 2-mol% Sb ₂ O ₃	78
5.21	Sb ₂ O ₃ content dependence of energy band-gap of the ZnO	79



LIST OF ABBREVIATIONS

BPPE	Back-detection PPE
C-V	Capacitor-Voltage
DLTS	Deep-level transient spectroscopy
DSB	Double Schottky Barrier
EMR	Electromagnetic radiation
FPPE	Front-detection PPE
He-Ne	Helium-Neon
ICTS	Isothermal capacitance transient spectroscopy
IPPE	Inverse PPE
I-V	Current-Voltage
NC-BPPE	Non-Contact-Back PPE
NC-FPPE	Non-Contact-Front PPE
PA	Photoacoustic
PAS	Photoacoustic spectroscopy
PE	Pyroelectric
PPE	Photopyroelectric
PPES	Photopyroelectric spectroscopy
PSD	Phase-sensitive-detection
PT	Photothermal
PVA	Polyvinyl alcohol
PVDF	Polyvinylidene diflouride
RPPE	Reflective PPE



SEM	Scanning electron microscopy
SPPE	Standard PPE
XRD	X-ray diffraction



LIST OF SYMBOLS

α	Thermal diffusivity
β	Optical absorption coefficient
С	Specific heat
е	Thermal effusivity
E_g	Energy gap
Е	Dielectric constant
\mathcal{E}_{0}	Vacuum permittivity
f	Modulation frequency
hv	Quantized photon energy
i	√-1
Io	Optical intensity
k	Thermal conductivity
l_{eta}	Optical absorption length
т	Slope or gradient
L	Thickness
λ	Wavelength of light
η	Light-to-heat conversion efficiency
р	Pyroelectric coefficient
ρ	Density
Q_o	Heat source intensity
R_n	Thermal wave reflection coefficient
$R(\lambda)$	Optical reflectivity at wavelength λ
T_n	Thermal wave transmission coefficient
μ.	Thermal diffusion length
ω	Angular modulation frequency.
С	Speed of light
V	Voltage
ℓ_d	Film thickness
ΔT	Temperature rise



r	Thermal resistance
γ	Nonlinearity coefficient
V_{th}	Thermal voltage
υ	Frequency
h	Planck's constant
β_s	Optical absorption coefficient of sample
eta_p	Optical absorption coefficient of pyroelectric film
$\mu_{eta s}$	Optical absorption depth of sample
$\mu_{eta p}$	Optical absorption depth of pyroelectric film





CHAPTER 1

INTRODUCTION

1.1 Introduction

This thesis is presented in six chapters. The First Chapter is the general Introduction. Chapter Two discusses the literature review of the previous work for the photothermal and structural characterization of ZnO based ceramic. Chapter Three is a review of photothermal (PT) characterization theory including the thermal diffusivity measurement using pyroelectric (PE) technique, the spectrometer and a brief explanation about the optical band-gap energy. Chapter Four is concerned with the measurement set-up and apparatus. The sample preparation of ZnO ceramic is also discussed in this chapter. Chapter Five presents the results obtained through experiments conducted in the Photoacoustic (PA) Laboratory of Physics Department at Universiti Putra Malaysia of photopyroelectric (PPE) spectroscopy. Finally, Chapter Six summarizes the work conducted in this thesis and presents recommendations for future work pertaining to the area of photopyroelectric (PPE) characterizations on ceramic sample especially for ZnO sample which has wide variety of applications.

1.2 Motivation and Problem Statement

This thesis is concerned with the topic of PPE study of ZnO ceramics. One of its wide applications is as a varistor in electronic ceramic materials area whose electrical behavior is dominated by grain-boundary interface states. Many research studies that



are concerned with the grain boundary of ZnO ceramics have been performed. It has been confirmed that the electrical behavior of ceramics is closely related to the Double Schottky Barrier (DSB) formed at the grain boundary. The donor density has been determined using the modified C-V characteristics and infrared reflection spectrum. The bulk traps on ZnO varistors have also been characterized by many researchers. Also, much attention has been paid to the interface states which directly affect the nonlinear I-V characteristics of ZnO varistors and are closely related to the formation of DSB. The interface states have been investigated using transient capacitance methods such as deep-level transient spectroscopy (DLTS) and isothermal capacitance transient spectroscopy (ICTS).

In spite of the many investigations carried out on ZnO varistors, detailed analysis of the defects and associated states has not been sufficiently elucidated. Although numerous investigations have been carried out on the electrical properties, few investigations concern the relationship between the optical absorption and the I-V characteristics for ceramic ZnO containing metal impurities because of the difficulty with the conventional transmission methods due to strong scattering. PT spectroscopy such as PPE and PA spectroscopy is the useful tool to study the optical absorption spectra of ceramic ZnO containing suitable metal oxides. Using these methods, a study of the non-radiative recombination processes and the evaluation of the optical and thermal properties of materials can be conducted. It is also effective for non-contact detection of the energy state and the deep level in the scattering sample such as ceramics and powders.



1.3 Objectives

The objectives of this research are:

- 1. To investigate the thermal diffusivities of zinc oxide doped with bismuth oxide using the pyroelectric method, and
- 2. To determine the band-gap energy of zinc oxide doped with transition metal material by using photopyroelectric method.

3



CHAPTER 2

LITERATURE REVIEW

2.1 Introduction

The photopyroelectric (PPE) technique is one of the useful methods to determine the thermal parameters of a sample such as thermal diffusivity and to investigate optical properties of materials. This technique is based on a photothermal effect where a pyroelectric (PE) transducer is used to detect the temperature variation from a light-induced periodic heating in a sample. The transducer possesses a temperature-dependent spontaneous polarization below the Curie temperature that changes as the temperature of a material change (Blackburn, 1970). When there is absorption of incident light, the non-radiative de-excitation processes within the solid cause the sample temperature to fluctuate and, through heat diffusion to the surrounding pyroelectric film, the temperature of the sample-PE film interface fluctuates (John *et al.*, 1986). Due to this temperature change, a PE voltage is produced in the PE film and is given by;

$$V = \frac{pl_d}{\varepsilon} \Delta T \tag{2.1}$$

where *p* is the PE coefficient of the film, l_d is the film thickness, ε is the film dielectric constant and ΔT is the temperature rise in the film (John *et al.*, 1986).

Zinc oxide varistors are ZnO-based ceramic semiconductor devices with highly nonlinear current-voltage characteristics (Levinson *et al.*, 1986). The varistors are



typically fabricated by sintering of ZnO with small amounts of additives with other metal oxides material such as Bi₂O₃, CoO, MnO, Sb₂O₃, SnO₂, Cr₂O₃ and etc. These additives are the main tools that are used to improve the nonlinear response and the stability of ZnO. Many authors reported that the Bi₂O₃ are typically used at the first stage of varistor fabrication. Wong (1980) reported that the Bi₂O₃-rich liquid phase enhanced densification during the initial stages of sintering and also increased the final grain size of the resulting ZnO structures.

This chapter is concerned with the review of the evolution of PPE techniques for the optical and thermal purpose. The overview will also mention the ZnO as a varistor and the significant characterizations.

2.2 Review on Thermal Diffusivity of ZnO-Based Ceramic

Historically, the search for PE materials has been focused on their infrared radiation detectivity and their efficient high frequency responsivity (Bergman *et al.*, 1971). The most commonly used PPE configurations are shown in Figure 2.1. In standard PPE (SPPE) configuration, the modulated radiation is illuminated on the front surface of the sample, refer to Figure 2.1 (a). The PE sensor is in thermal contact with rear side of the sample. It is also known as back-detection PPE (BPPE) because the detect signal relies on the diffusion of the heat across the sample. Quantitative description of the basis phenomena in SPPE detection which was given by Mandelis and Zver (1985) shows that the particularization of the general PPE responses leads to six special cases based upon the optical, thermal and physical thickness of the sample. Chirtoc and Mihailescu (1989) mark a step further to consider the role

