UNIVERSITI PUTRA MALAYSIA

DIRECT BLOCK METHODS FOR SOLVING SPECIAL SECOND ORDER ORDINARY DIFFERENTIAL EQUATIONS AND THEIR PARALLEL IMPLEMENTATIONS

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FS 2008 18

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By

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Thesis Submitted to the School of Graduate Studies, Universiti Putra Malaysia, in Fulfilment of the Requirements for the Degree of Master of Science

March 2008

Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfilment of the requirement for the degree of Master of Science

DIRECT BLOCK METHODS FOR SOLVING SPECIAL SECOND ORDER ORDINARY DIFFERENTIAL EQUATIONS AND THEIR PARALLEL IMPLEMENTATIONS

By

YAP LEE KEN

March 2008

Chair : Associate Professor Dr Fudziah Binti Ismail, PhD

Faculty : Science

This thesis focuses mainly on deriving block methods of constant step size for solving special second order ODEs. The first part of the thesis is about the construction and derivation of block methods using linear difference operator. The regions of stability for both explicit and implicit block methods are presented. The numerical results of the methods are compared with existing methods. The results suggest a significant improvement in efficiency of the new methods.

The second part of the thesis describes the derivation of the *r*-point block methods based on Newton-Gregory backward interpolation formula. The numerical results of explicit and implicit *r*-point block methods are presented to illustrate the effectiveness of the methods in terms of total number of steps taken, accuracy and execution time. Both the explicit and implicit methods are more efficient compare to the existing method.

The *r*-point block methods that calculate the solution at *r*-point simultaneously are suitable for parallel implementation. The parallel codes of the block methods for the solution of large systems of ODEs are developed. Hence the last part of the thesis discusses the parallel execution of the codes.

The parallel algorithms are written in C language and implemented on Sun Fire V1280 distributed memory system. The fine-grained strategy is used to divide a computation into smaller parts and assign them to different processors. The performances of the *r*-point block methods using sequential and parallel codes are compared in terms of the total steps, execution time, speedup and efficiency. The parallel implementation of the new codes produced better speedup as the number of equations increase. The parallel codes gain better speedup and efficiency compared to sequential codes.

Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia sebagai memenuhi keperluan untuk ijazah Master Sains.

KAEDAH BLOK LANGSUNG BAGI MENYELESAIKAN PERSAMAAN PEMBEZAAN KHAS PERINGKAT KEDUA DAN IMPLEMENTASINYA SECARA SELARI

Oleh

YAP LEE KEN

March 2008

Pengerusi : Associate Professor Dr Fudziah Binti Ismail, PhD

Fakulti : Sains

Tumpuan utama tesis ini adalah untuk menerbitkan kaedah blok dengan saiz langkah malar untuk menyelesaikan persamaan pembezaan khas secara langsung. Bahagian pertama tesis ini adalah berkaitan dengan pembentukan dan terbitan kaedah blok dengan menggunakan pengoperasi beza linear. Rantau kestabilan untuk kedua-dua kaedah tersirat dan kaedah tak tersirat turut dipersembahkan. Keputusan berangka kaedah tersebut dibandingkan dengan kaedah yang sedia ada. Keputusan berangka menunjukkan penambahbaikan yang ketara dalam kecekapan kaedah baharu tersebut.

Bahagian kedua tesis ini menghuraikan terbitan kaedah blok *r*-titik berdasarkan formula sisipan belakang Newton-Gregory. Keputusan kaedah *r*-titik tersirat dan kaedah *r*-titk tak tersirat telah ditunjukkan untuk mengilustrasi keberkesanan

kaedah dari segi jumlah langkah yang diambil, kejituan dan masa pelaksanaan. Kedua-dua kaedah tersirat dan kaedah tak tersirat adalah lebih cekap berbanding dengan kaedah yang sedia ada.

Kaedah blok *r*-titik yang mengira penyelesaian pada *r*-titik serentak adalah sesuai untuk implementasi selari. Kaedah blok dengan kod selari untuk penyelesaian sistem persamaan pembezaan telah dibangunkan. Seterusnya bahagian akhir tesis ini membincangkan kod implementasi selari tersebut.

Algoritma selari ditulis dalam bahasa C dan dilaksana di sistem memori bertaburan Sun Fire V1280. Strategi *fine-grained* digunakan untuk membahagi perhitungan ke bahagian-bahagian kecil dan menugaskan bahagian-bahagian kecil ini ke pemproses yang berlainan**.** Implementasi kaedah blok *r*-titik yang menggunakan kod jujukan dan kod selari dibandingkan dari segi jumlah langkah, masa pelaksanaan, kecepatan dan keberkesanan. Kod selari kaedah baru menghasilkan kecepatan yang lebih baik apabila bilangan persamaan bertambah. Kod selari mencapai kecepatan dan kecekapan yang lebih baik berbanding dengan kod jujukan.

ACKNOWLEDGEMENTS

First and foremost, I would like to show my deepest appreciation and gratitude to the Chairman of the Supervisory Committee, Associate Professor Dr Fudziah Binti Ismail for her invaluable assistance, advice and guidance throughout the duration of the studies. I also wish to express my sincere thank to Associate Professor Dr Mohamed Bin Othman and Yang Berbahagia Professor Dato' Dr Mohamed Bin Suleiman for their guidance towards the successful completion of the thesis.

Special thanks due to Universiti Putra Malaysia for providing the financial support in the form of Graduate Research Assistantship throughout the duration of my studies. The guidance and advice of Dr Zanariah Binti Majid are gratefully acknowledged.

Finally my deepest appreciation goes to my beloved family especially my parents for their unconditional love, support and understanding throughout the course of my studies. I also would like to thank my friends for their understanding support and encouragement throughout the course of my research.

I certify that an Examination Committee has met on 24 March 2008 to conduct the final examination of Yap Lee Ken on her degree thesis entitled "DIRECT BLOCK METHODS FOR SOLVING SPECIAL SECOND ORDER ORDINARY DIFFERENTIAL EQUATIONS AND THEIR PARALLEL IMPLEMENTATIONS" in accordance with Universiti Pertanian Malaysia (Higher Degree) Act 1980 and Universiti Pertanian Malaysia (Higher Degree) Regulations 1981. The Committee recommends that the student be awarded the Master of Science.

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This thesis was submitted to the Senate of Universiti Putra Malaysia and has been accepted as fulfilment of the requirement for the degree of Master of Science. The members of the Supervisory Committee were as follows:

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DECLARATION

I declare that the thesis is my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously, and is not concurrently, submitted for any other degree at Universiti Putra Malaysia or at any other institution.

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YAP LEE KEN

Date: 15 May 2008

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LIST OF ABBREVIATIONS

IVP	: Initial Value Problems
ODEs	: Ordinary Differential Equations
SISD	: Single Instruction Single Data
SIMD	: Single Instruction Multiple Data
MISD	: Multiple Instruction Single Data
MIMD	: Multiple Instruction Multiple Data
CPUs	: Central Processing Units
MPI	: Message Passing Interface
E2P1B	: Explicit 2-Point 1-Block
E3P1B	: Explicit 3-Point 1-Block
I2P1B	: Implicit 2-Point 1-Block
I3P1B	: Implicit 3-Point 1-Block
E1P	: Explicit 1-Point
E2PB	: Explicit 2-Point Block
E3PB	: Explicit 3-Point Block
I1P	: Implicit 1-Point
I2PB	: Implicit 2-Point Block
I3PB	: Implicit 3-Point Block
PE2PB	: Parallel Explicit 2-Point Block
PI2PB	: Parallel Implicit 2-Point Block
PE3PB	: Parallel Explicit 3-Point Block
PI3PB	: Parallel Implicit 3-Point Block