



**UNIVERSITI PUTRA MALAYSIA**

**ANALYSIS OF THRUST DENSITY CALCULATION FOR LINEAR DC  
ACTUATORS**

**NOOR AZITA BT AWALUDIN**

**FK 2006 111**



**ANALYSIS OF THRUST DENSITY CALCULATION FOR LINEAR DC  
ACTUATORS**

**By**

**NOOR AZITA BT AWALUDIN**

**Thesis Submitted to the School of Graduate Studies, University Putra Malaysia, in  
Fullfilment of the Requirement for the Degree of Master of Science**

**July 2006**



**DEDICATED TO:  
MY FAMILY AND HAMDAN**



## TABLE OF CONTENTS

		<b>Page</b>
	<b>DEDICATION</b>	
	<b>ABSTRACT</b>	2
	<b>ABSTRAK</b>	4
	<b>ACKNOWLEDGEMENTS</b>	6
	<b>APPROVAL</b>	7
	<b>DECLARATION</b>	9
	<b>LIST OF TABLES</b>	10
	<b>LIST OF FIGURES</b>	13
	<b>LIST OF ABBREVIATIONS</b>	15
 <b>CHAPTER</b>		
I	<b>INTRODUCTION</b>	15
II	<b>LITERATURE REVIEW</b>	24
	Previous research study	24
	Development of Linear actuator	24
	Introduction of Linear actuator	27
	Theory of Magnetic Circuit	28
	Simple magnetic circuit without air gap	28
	Simple magnetic circuit with air gap	32
	Basic operation of Electromagnet Actuator	35
	Basic operation of Permanent Magnet Actuator	38
III	<b>THRUST DENSITY CALCULATION</b>	41
	Introduction	41
	Thrust density calculation of Electromagnet Actuator	43
	Flux distribution	43
	Coil calculation	48
	Thrust calculation	50
	Dimension calculation	55
	Thrust density calculation	57
	Thrust density calculation of Permanent Magnet Actuator	60
	Dimension calculation	60
	Flux distribution	63
	Calculation of moving coil electromotive force	67
	Thrust density calculation	67
	Comparison on derivation for linear DC actuator	71
IV	<b>THRUST CHARACTERISTICS OF LINEAR DC ACTUATORS</b>	74
	Introduction	74
	Thrust measurement of Electromagnet Actuator	77



	Prototype	77
	Thrust measurements	79
	Results	80
	Plotted results	82
	Thrust measurement of Permanent Magnet Actuator	83
	Prototype	83
	Results	86
	Thrust measurement	87
	Comparison of measured and calculation results of thrust	89
	Electromagnet Actuator	89
	Permanent Magnet Actuator	92
<b>V</b>	<b>CONCLUSIONS</b>	
	Conclusions	95
	<b>REFERENCES</b>	100
	<b>APPENDICES</b>	103
	<b>BIODATA OF THE AUTHOR</b>	123



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in fulfillment of the requirement for the degree of Master of Science

**ANALYSIS OF THRUST DENSITY CALCULATION FOR LINEAR DC ACTUATORS**

By

**NOOR AZITA BINTI AWALUDIN**

**July 2006**

**Chairman : Norhisam Misron, PhD**

**Faculty : Engineering**

In recent years, researcher has developed many actuators with different configurations depending on application required. Linear actuator has become one of the most popular actuator used in industry especially in factory automation. Linear motor, which have a compact and simple structure are easy to control compare to rotational motor [1]. The advantages of linear actuator are small size, low power and high thrust. The thrust of linear motor can be applied on to the load without any mechanical loss as rotation motor. But then, the generation of thrust produced by linear actuators is barely being fully investigated. Therefore, problem arises in producing low cost machine but with higher thrust production.

A study was conducted with the objective to investigate thrust density characteristics in relation with dimension. Two designs were tested, that is Linear DC actuator using electromagnetic application and Linear DC actuator which using permanent magnet

application. The range of current supplied to wound coil is 1 A to 3 A, while permanent magnet produced magnetic flux directly.

Expressions on the thrust generation on both linear actuators were derived in relation with the dimension and size of the machine. Derivation was done based on a few assumptions that may constitute to the objectives of this study. For clarification purposes, experiment on both linear actuators was done depending on the physical condition. Through the experimental result, comparison can be made between theoretical and experimental result in order to find the thrust density characteristic of linear actuator.

Basically, the objective of this study is achieved when comparison that has been made for both type of linear actuator shows the largest error was only 20%. For future improvement, a few prototype of linear actuator with different configuration of closed loop path for the flux to flow can be made. This study only concentrated on the same closed loop path of flux flows with a few assumption have to be taken which are the temperature and type of material for yoke is neglected. It is important to take the a few assumptions in order to focus on the thrust density characteristics in relation with the dimension.

Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia sebagai memenuhi keperluan untuk ijazah Master Sains

**ANALISA KE ATAS KETUMPATAN DAYA TUJAHAN YANG DIHASILKAN  
OLEH PENDIKIT LINAR**

Oleh

**NOOR AZITA BINTI AWALUDIN**

**Julai 2006**

**Pengerusi : Norhisam Misron, PhD**

**Fakulti : Kejuruteraan**

Dalam beberapa tahun kebelakangan ini, ramai penyelidik telah mereka cipta pelbagai pendikit linar dengan bermacam konfigurasi. Pendikit arus terus telah menjadi semakin popular terutama dalam bidang perindustrian dan juga automasi. Motor linar yang mempunyai struktur yang padat dan ringkas adalah mudah untuk dikendalikan. Antara faedah motor linar ialah mempunyai saiz yang kecil, berkuasa rendah dan menghasilkan daya tujahan yang tinggi. Daya tujahan yang dihasilkan boleh digunakan secara langsung tanpa bantuan alat tambahan. Tetapi, kajian ke atas penghasilan daya tujahan berbanding dengan saiz fizikal adalah kurang diberi perhatian. Oleh itu, timbul masalah dimana penghasilan mesin yang murah tetapi boleh memberi daya tujahan yang tinggi.

Oleh itu, satu kajian telah dijalankan dengan objektif untuk mengkaji karektor ketumpatan daya tujahan. Dua rekabentuk telah diuji, iaitu Pendikit Arus Terus Linar yang menggunakan aplikasi elektromagnet dan juga Pendikit Arus Terus Linar yang



menggunakan aplikasi magnet kekal. Julat arus adalah dari 1 A hingga 3 A, manakala magnet kekal menjana arus magnet dengan sendirinya.

Formula untuk daya tujahan bagi kedua-dua prototaip telah diuraikan dengan saiz atau dimensi sesuatu mesin telah dilakukan. Formula tersebut dihuraikan bersama-sama dengan beberapa anggapan yang sesuai. Untuk tujuan mengesahkan ketepatan nilai yang telah dikira, eksperimen telah dijalankan ke atas kedua-dua prototaip. Melalui eksperimen tersebut, perbandingan diantara nilai teori dan nilai eksperimen telah dilakukan untuk menganalisis karektor daya tujahan yang telah dihasilkan.

Secara umumnya, objektif kajian ini telah dicapai apabila perbandingan yang dilakukan antara nilai teori dan eksperimen menunjukkan ralat yang paling besar hanyalah sebanyak 20% sahaja. Untuk masa hadapan, kajian boleh dilakukan untuk konfigurasi laluan garis medan magnet yang tertutup yang berlainan. Untuk kajian ini, konfigurasi yang serupa sahaja dilakukan. Ini bertujuan untuk memberi lebih fokus kepada daya tujahan yang dihasilkan berbanding faktor luar sebagai contoh; tahap kepanasan dan juga jenis bahan yang digunakan untuk membina teras.

## ACKNOWLEDGEMENTS

PRAISES and THANKS belong only to ALLAH for giving the author time and health to work together with fellow researchers and friends in completing the study.

High appreciation is given to Dr. Norhisam Misron, the chairman of the supervisory committee for his guidance during the period of study. The author also wishes to thank fellow lecturer, who has given a lot of advice and guidance to ensure that he can complete this study within the targeted period and to Dr. Syed Javaid Iqbal for the cooperation .

This study could not be completed successfully without valuable assistance from En. Megat Nasaruddin dan En. Azrul Edry. Thanks to laboratory assistance that the authors cannot mention. Their kindness and cooperation in allowing the author to use the laboratory is very much appreciated.

Thanks to MARA for providing financial support to the author. Last but not least, the author is particularly grateful to her beloved family: her father, her brothers and sisters in law. All the advice and moral support is very much appreciated.



I certify that an Examination Committee met 11 July 2006 to conduct the final examination of Noor Azita Awaludin on her Master of Science thesis entitled “Analysis of Thrust Density for Linear DC Actuators” in accordance with Universiti Pertanian Malaysia (Higher Degree) Act 1980 and Universiti Pertanian Malaysia (Higher Degree) Regulations 1981. The Committee recommends that the candidate be awarded the relevant degree. Members of the Examination Committee are as follows:

**Mohd Adzir Mahdi, PhD**

Associate Professor  
Faculty of Engineering  
Universiti Putra Malaysia  
(Chairman)

**Senan Mahmod Abdullah, Ph.D**

Associate Professor  
Faculty of Engineering  
Universiti Putra Malaysia  
(Internal Examiner)

**Samsul Bahari Mohd Noor, Ph.D**

Faculty of Engineering  
Universiti Putra Malaysia  
(Member)

**Ir. Abdul Halim Mohamed Yatim, PhD**

Professor  
Faculty of Engineering  
Universiti Putra Malaysia  
(External Examiner)

---

**HASANAH MOHD. GHAZALI, PhD**

Professor/Deputy Dean  
School of Graduates Studies  
Universiti Putra Malaysia

Date: 22 November 2006



This thesis submitted to the Senate of Universiti Putra Malaysia and has been accepted as fulfilment of the requirement for the degree of Master Science. The members of the Supervisory Committee are as follows:

**Norhisam Misron, PhD**

Lecturer

Faculty of Engineering

Universiti Putra Malaysia

(Chairman)

**Syed Javaid Iqbal, PhD**

Lecturer

Faculty of Engineering

Universiti Putra Malaysia

(Member)

---

**AINI IDERIS, PhD**

Professor/Dean

School of Graduate Studies

Universiti Putra Malaysia

Date: 14 DECEMBER 2006

## **DECLARATION**

I hereby declare that the thesis based on my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously or concurrently submitted for any other degree at UPM or other institutions.

---

**NOOR AZITA BT AWALUDIN**

Date: 17 NOVEMBER 2006



## LIST OF TABLES

<b>Table</b>		<b>Page</b>
2.1	Comparison of electrical and magnetic quantities	30
3.1	Different condition for $l_g, 2l_{by1}$ and $2l_{by2}$ on thrust calculation	53
4.1	Specification of designed LDA	78
4.2	The thrust generated in 200 turns of moving coil	81
4.3	The thrust generated in 300 turns of moving coil	81
4.4	Specification of designed LDM	84
4.5	Measurement of thrust for LDM	87

## LIST OF FIGURES

<b>Figure</b>		<b>Page</b>
1.1	Flowchart for general procedure	16
1.2	Flux potential in Electromagnet Actuator	19
1.3	Flux potential in Permanent Magnet Actuator	21
2.1	Simple magnetic structure	31
2.2	Analogous comparison between electrical and magnetic circuit	31
2.3	Series magnetic circuit	33
2.4	Simple magnetic structure with an air gap	34
2.5	Basic structure of Electromagnet Actuator	36
2.6	Dimension of Electromagnet Actuator	37
2.7	The direction of thrust on the upper half of Electromagnet Actuator	37
2.8	Basic structure of Permanent Magnet Actuator	39
2.9	Dimension of Permanent Magnet Actuator	30
2.10	The direction of thrust on the upper half of Permanent Magnet Actuator	40
3.1	Thrust and overall volume of the machines	43
3.2(a)	Magnetic analysis on Electromagnet Actuator	44
3.2(b,c)	Magnetic analysis on Electromagnet Actuator	45
3.3	Cross section half of stator coils	49
3.4	Graph of magnetic density versus the stator current	51
3.5	Calculation of thrust characteristics	54
3.6	Dimension parameters in Electromagnet Actuator model	56



3.7	The total flux flow in the air gap	56
3.8(a,b)	The thrust density characteristics on Electromagnet Actuator	58
3.8(c)	The thrust density characteristics on Electromagnet Actuator	59
3.9(a)	Dimension and flux path of Permanent Magnet Actuator model	62
3.9(b)	Dimension and flux path of Permanent Magnet Actuator model	63
3.10	Flux line and flux distribution in Permanent Magnet Actuator	64
3.11	<i>B-H</i> curve of permanent magnet in Permanent Magnet Actuator model	66
3.12	Relation of Permanent Magnet Actuator thrust and motor volume	69
3.13	Thrust density versus motor volume	70
3.14	Comparison on thrust density between Electromagnet Actuator and Permanent Magnet Actuator	73
4.1	General step for experimental procedure	76
4.2	Prototype of Electromagnet Actuator	78
4.3	Experimental set-up for Electromagnet Actuator	80
4.4	The characteristics of thrust measurement	83
4.5	Prototype of Permanent Magnet Actuator	84
4.6	The characteristics of the thrust measured in different displacement	86
4.7	Experimental set-up for Permanent Magnet Actuator	88
4.8	Thrust characteristics in different displacement	89
4.9	The comparison of calculation and measurement value	90
4.10	Characteristics of thrust density in Electromagnet Actuator	91
4.11	The calculation and measurement value of thrust density characteristics	93
4.12	Characteristics of thrust versus the moving coil current	94





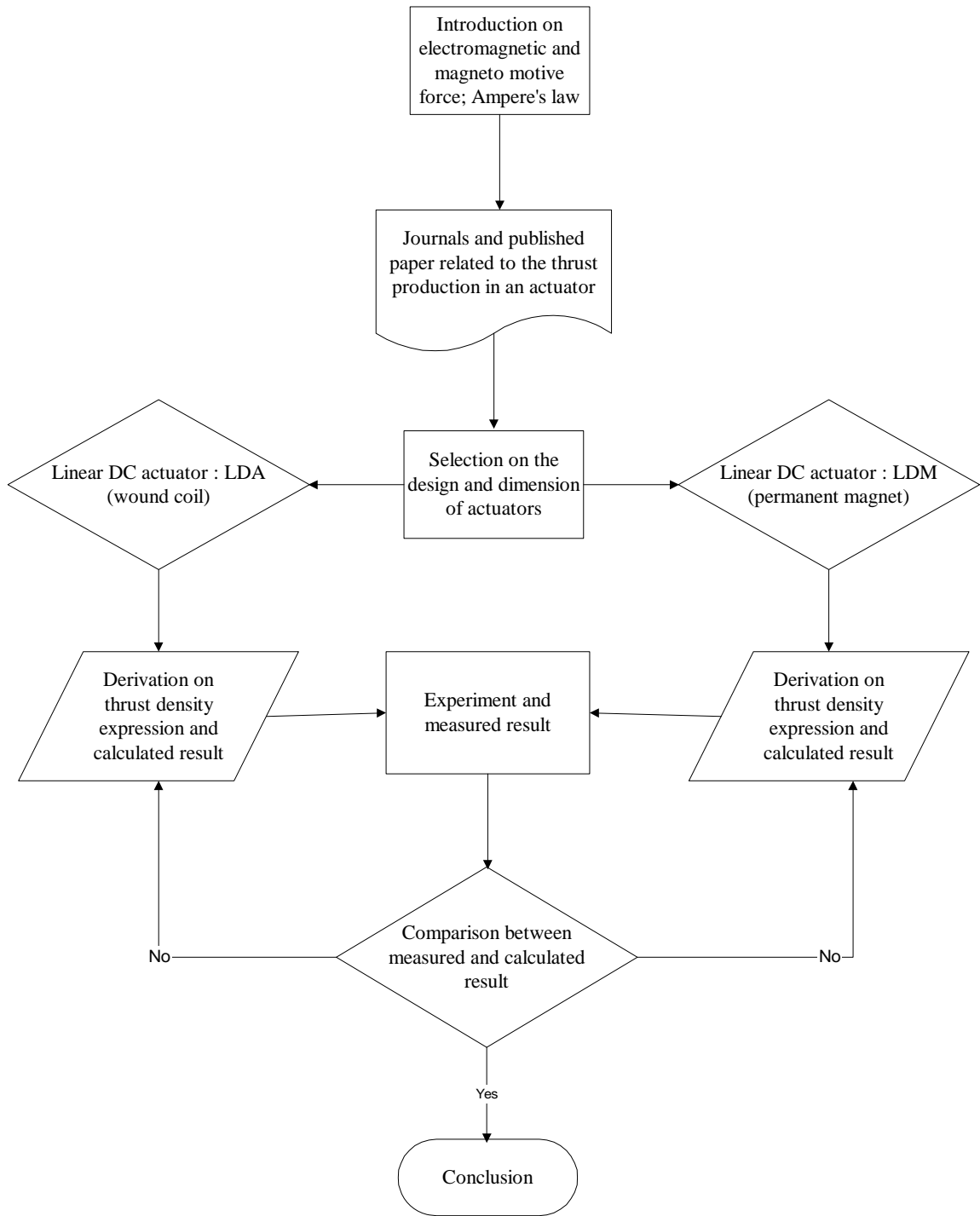


# CHAPTER 1

## INTRODUCTION

Nowadays, linear motor become one of the most demanding machine in industry especially automation and factories. The demand of linear motor become increasing since the advantages that could benefits industry mainly in production cost. The design optimization of magnetic systems has been an important issue [1,2]. Among various components of magnetic systems, coil is the component that investigation is concerned [3]. Studies on linear motors and actuator have been well established by previous researcher in order to improve the quality and performance of production in industries involved. Among the advantages that can be provided by linear motor is small and easy to operate besides its ability to give the amount of power required. Usually, the structure of linear motors and linear actuators is simple and easy to understand. Although a few studies have been made on linear actuators, none of them has considered the thrust generation with relation to the dimension or the size of the machines. Therefore, this study is done on the main basis of the thrust generation to the dimension of the machine. In order for future development, the size of the machine can be reduced but producing a higher thrust density. This will give more advantages for industries in term of cost of production. Fig. 1.1 shows the flowchart of this study.





**Figure. 1.1: Flowchart for general procedure done on study of Analysis of Thrust Density on Linear DC Actuator**

Basically, linear actuator consists of wound coil supplied with current which act as stator and also permanent magnet itself. It does not need any auxiliary parts to operate such as gears or oscillating equipments. Linear actuator is an electromechanical devices which produce unidirectional or bidirectional short-stroke (less than a few meters) motion. Linear motions refer to a straight line motion [4].

Basically in linear actuator, its principle is based on the electromagnetic field theory, Maxwell's equations and Ampere's law. Naturally, these equations govern the electromagnetic phenomena in energy conversion devices [5]. Conventionally, when a conductor of length  $l$  carries a current  $I$  in a direction perpendicular to a magnetic field of flux density  $B$ , the conductor experience a force  $F$  perpendicular to both the direction of current flow and the magnetic field. This force is given by [5]

$$F = IBl$$

for a single wound conductor. In case of a linear motor, the magnitude of force produced is given by [5]

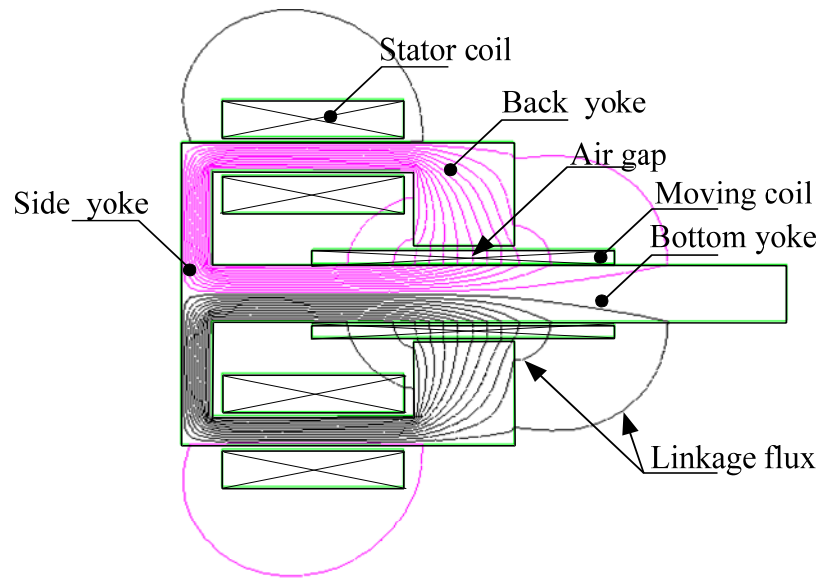
$$F = NIBl$$

where  $N$  is the number of turns of the conductor.

These basic equations of force or refer as thrust from now onwards, can be converged to a new formula with a few assumptions. Generally the computation of the total force is a natural extension of the local force calculation [6]. The main assumptions that have been made are excluding the temperature rise in the motor and there is no power loss or known as an ideal condition. Therefore, the equations may lack from a few basic supporting factors that effected the calculation, but it is important for us to bear in mind

that the main point of this study is to make a comparison between the thrust generated with the calculated thrust's value in relation with the dimension of the actuator.

In the first scenario of magnetic fields applications, linear actuator using the electromagnetic application is used. From now onwards it is known as Electromagnet Actuator only for reference purposes in this study. Basically, this actuator is become widely use in factory and office appliances such as coffee machine or sliding door. Its simple structure and easy to control are among the advantages that can be offered. Linear actuators also gives a low production cost with highest thrust produced besides the fact that thrust can be directly used without additional auxiliary devices such as gears. A high precision positioning system generally adopts a linear motor as an actuator [7]. Using the basic concepts of Ampere's law, the equation of thrust produced in relation with the dimension of the electromagnet actuator can be derived. The main assumption taken was that the amount of the flux flow from the yoke of electromagnet actuator to air gap is same as the amount of the flux flow from air gap to the yoke again as shown in Fig.1.2. Therefore the thrust expression for electromagnet actuator is derived in this study. This expression shown the relationship between the magnetic densities produced with the dimension of the electromagnet actuator.



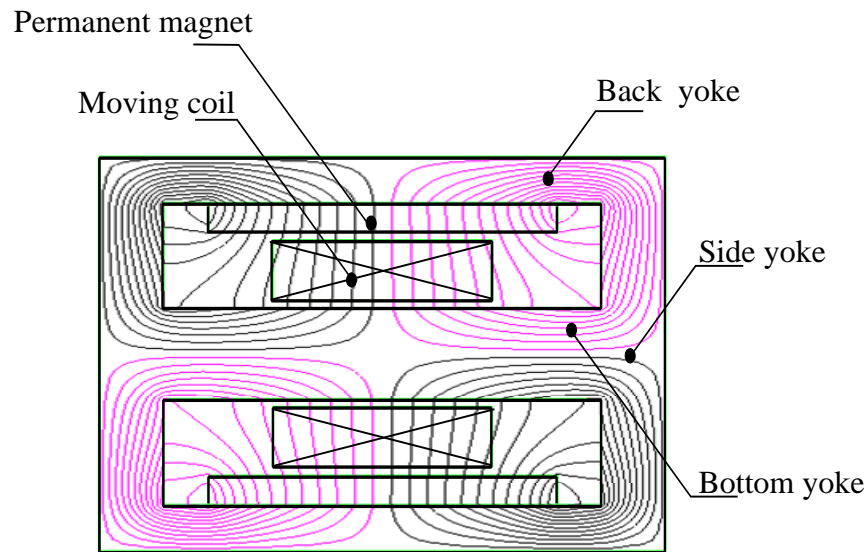
**Figure. 1.2: Flux potential in electromagnet actuator**

Using the equation derived, thrust calculation was derived by differentiation on the dimension of the electromagnet actuator. As a result, this calculated value can be compared to the experimental value, which is done by measuring the thrust produced in electromagnet actuator using the digital scale. Theoretically, the experiment value is expected to have nearly the same value with the calculation. The thrust characteristic for both experimental and calculation value is plotted and error analysis was made.

Mainly, for the second scenario of magnetic fields applications is using the permanent magnet in Linear DC actuator instead of wound coil supplied by current to act as stator as shown in Fig. 1.3. For reference purposes in this study, the actuator now and onwards is referred as permanent magnet actuator. The permanent magnets have been extensively used to replace the excitation winding in synchronous machines with the advantages of

simple rotor design without field windings, slip rings and exciter generator, avoiding heat dissipation in the rotor and providing higher overall efficiency [8]. As known for the last few decades, the energy density of permanent magnets becomes improved with development of new materials. Basically, when using the permanent magnet, the most important thing to consider is the properties of the permanent magnet. The properties of the permanent magnet can be seen from the relationship between the flux density or magnetic density,  $B$ , and the magnetizing field strength,  $H$ , may be represented by the hysteresis loop. Besides the hysteresis loop, the permeance coefficient,  $p$ , also an important factor for applications of permanent magnet. The size of the Linear DC motor (permanent magnet actuator) is the main consideration in order to have small permanent magnet actuator but produced high thrust. As a result, through these factors, derivation on the thrust expression for permanent magnet in relation with the volume of permanent magnet actuator can be made. The thrust expression is derived. For permanent magnet actuator, the characteristic of thrust density is studied through the thrust and the volume of permanent magnet actuator. A few graphs was plotted in order to clarify the measurement value with calculated value of thrust. Dimension of permanent magnet actuator becomes the main parameter where the thrust density is related to the dimension of permanent magnet actuator, which means that the thrust generated in permanent magnet actuator can be calculated given the size of the motor.

Conclusion on both motor was made depending on the analysis of thrust characteristics and thrust density characteristics of respective linear dc actuators. Mainly, the objectives of this study is achieved where the relationship between the size of motor and the thrust generated become the main priority.



**Figure 1.3: Flux potential in permanent magnet actuator**

Methodologically, the analysis was done by conventional experiment and also through Finite Element Method (FEM). Nowadays, advanced research studies commonly employ standard FEM software packages for 3-D electromagnetic analysis and design [9]. FEM was used in order to see the magnetic density contribution through out both motors. The FEM is different in that an approximation of the solution itself is sought over a specified domain: that of a finite size, geometrical volume called a finite element. This approximation is then introduced in the field equation or an equivalent form of the field equations.

For modeling using FEM, the model of the designed actuator has to be drawn using software known as Microcal Origin. This modeling will be referred in creating three



kind of file which are the bod, blk and mesh file. These file consists of information on the modeling structure in terms of numbers and coordinates. Then, element calculation is done by using software known as V mesh. It composes those three files within fra file. It calculates the element in the modeling structure. Then, fra file will be converted to mesh file using another software known as Cygwin. This software will show the element in the model in 2D. For magnetic analysis, a config file needs to be prepared. This file is a reference for femaph.exe for calculation. The config file consists of certain value of parameter that relates femaph.exe about the material of each block structure and even the magnetic properties. This parameter can be change for each different simulation. If magnetic analysis is successful, the results can be shown directly on the designed model as shown in Fig 1.2 and 1.3. It shows the flux potential in the motor which represented by different color of lines. This differences show two kinds of magnetic potentials which is North (N) and South (S). It is important to analyze the magnetic flux distribution in order to see the flux flow according to theoretical assumption. As a result, a strong expression derived based from the analysis done using FEM.

Both prototype of electromagnet actuator and permanent magnet actuator was built and used to measure the thrust density generated in every case. The size and dimension of prototype was set to be as small as it can be, so that the impact of thrust generated in the prototype can be seen. Referring to the volume, the thrust generated experimentally can be plotted and compared to the calculated value of thrust and the error can be calculated.

For experimental analysis, the set-up of both electromagnet actuator and permanent magnet actuator is the same where the thrust generated was measured using the digital