

#### **UNIVERSITI PUTRA MALAYSIA**

# THE PERFORMANCE AND KINETIC STUDY OF MEMBRANE ANAEROBIC SYSTEM (MAS) IN TREATING POME

LAI LONG SENG

FK 1999 15



## THE PERFORMANCE AND KINETIC STUDY OF MEMBRANE ANAEROBIC SYSTEM (MAS) IN TREATING POME

By

#### LAI LONG SENG

Thesis Submitted in Partial Fulfilment of the Requirements for the Degree of Master of Science in Faculty of Engineering, Universiti Putra Malaysia

November 1999



#### **ACKNOWLEDGEMENT**

I am particularly grateful to my supervisor, Assoc. Prof. Dr. Fakhru'l – Razi Ahmadun who has helped me to complete this project. Your helping word to me in my difficulties is like a switch on a railroad track- but one inch between a wreck or smooth rolling prosperity. I wish to express my deepest thank and appreciation for your invaluable guidance, keen interest, advice, unreserved assistance and encouragement throughout the period of this study. Appreciation also goes to members of my supervisory commitee, Assoc. Prof. Dr. Mohd. Ali Hassan and Assoc. Prof. Dr. Azni Idris for their kind assistance in this study.

I also wish to extend my appreciation to En. Ismail Ghani and En. Mohd. Taufik for their technical support throughout this study. To the staffs in Fakulti Kejuruteraan, I wish to express my gratitude for being so kind in helping me in many ways to complete this study.

Last but not least, I like to thank Mum, Dad, Fook, Wee, Choo and Min for their love, understanding and steadfast. Special thanks to my fiancee, May, for her patience supports and loving encouragement. To all the brothers and sisters of The Church in Kajang, thank you for your love and care during my time in UPM.



## **TABLE OF CONTENTS**

		Page
ACKNOWL	EDGEMENT	ii
LIST OF TA	BLES	v
		vi
	GURES	
LIST OF PL	ATES	viii
LIST OF AB	BREVIATIONS	ix
ABSTRACT		x
ABSTRAK		xii
CHAPTER I	INTRODUCTION	1
	OBJECTIVES	2
П	LITERATURE REVIEW  Biological Treatment  Biochemistry and Microbiology  First Step: Hydrolysis  Second Step: Acidogenesis  Third Step: Acetogenesis  Fourth Step: Methanogenesis  Anaerobic Digestion	3 5 5 6 6 7 10
	Anaerobic Process Control	13
	Temperature	13
	pH	15
	Mixing	
	Alkalinity Kinetic and Modelling	16 17
	Biological Growth Kinetic	17
	Growth Rate	17
	Growth Yield and Substrate Utilisation Rate	18
	Effect of Substrate Concentration on the	40
	Microbial Growth Rate	19
	Continuous Culture Models  The Rate Limiting Step	22 23
	The Rate Limiting Step  Membrane Process	23
	Membrane Senaration in Rioreactor	27



	Polarization and Membrane Fouling	29
Ш	MATERIAL AND METHODOLOGY	32
	Sample	32
	Seed Sludge	3.
	Experimental Design	3.
	Operating Procedure	34
	Laboratory Analysis	3
	Gas Measurement	3
	Start-up	3
	Steady State	3
	First Attempt	3
	Second Attempt	3
	Membrane Cleaning	4
	DEGLE EG AND DEGGEGGGGGGG	
IV	RESULTS AND DISCUSSIONS	4
	Microbial Kinetics	4
	Comparison with Overall Kinetics and	_
	Summary of Intrinsic Kinetic Rates in Literature	5
	Reactor's Performance	5
	Gas Production and Composition	5
	COD Removal and System Efficiency	6
	COD Removal Efficiency Comparison	6
	With other Anaerobic Systems treating POME	,
	Change in Permeate Flux during the Study	6
	Determination of Minimum SRT	7
	Presence of Solids in Digester	7
V	CONCLUSIONS	7
V		
	Recommendation	7
REFEREN	ICES	8
APPENDI	CES	8
	pecification of the Reactor	8:
A SI	Confederation of the reactor	0.
ВЕх	sperimental Raw Data of TSS, VSS and Permeate COD	8
C Ex	sperimental Raw Data for Gas and Membrane Permeate Flux	8
VITA		Q



## LIST OF TABLES

	Table	Page
1	Typical Analysis of Palm Oil Mill Effluent	2
2	Kinetic Models Used in Anaerobic Treatment	23
3	Mathematical Expressions of Specific Substrate Utilization Rates for Kinetic Models	. 24
4	Anaerobic Solid-liquid Membrane Separation Bioreactors	31
5	Laboratory Analysis on Selected Parameters	. 35
6	Designated OLR, SRT and Sludge Wastage at Steady States	. 40
7	Mean Average Values of the Steady State Parameters	45
8	MAS Kinetic Coefficients	48
9	Representation Values of Kinetic Coefficients for Anaerobic Digestion at 35 <sup>0</sup> C	53
10	Comparison of Kinetic Coefficients between Khor's Study and this Study	. 53
11	Kinetic Coefficients of MAS Treating Raw POME	54
12	Kinetic Coefficients for Anaerobic Digestion of POME in Literature	. 55
13	Comparison between MAS and other Anaerobic Systems Treating POME	63
14	The Characteristics and Limitations of E and S at SRT for Each Model	71



## **LIST OF FIGURES**

	Figure	Page
1	Schematic Diagram of the Patterns of Carbon Flow in Anaerobic Digestion	7
2	Steps in the Anaerobic Digestion Process with Energy Flow	9
3	Typical Anaerobic Digestion:  (a) Conventional Standard-rate Single-stage Process;  (b) High-rate Complete-mix, Single-state Process;  (c) Two-state Process	11
4	The Common Anaerobic Treatment Systems in Treating the POME in Malaysia	12
5	Anaerobic Digestion Process based on Biomass Retention	14
6	Schematic Representation of a Membrane Process where the Feed Stream has been Separated into Retentate and Permeate Stream	25
7	An Overview of the Application of the Pressure Driven Membrane Processes in Relation to the Particle or Solute Size	26
8	Experimental Set-up	34
9	J- Tube Gas Analyzer	37
10	1/ SRT vs U	47
11	Monod Model	49
12	Contois Model	50
13 <sup>-</sup>	Chen and Hashimoto Model	51
14	Total Gas Production and CH4 Yield vs OLR	57
15	BLR, SUR and SSUR vs OLR	58



16	CH <sub>4</sub> Yield, % CH <sub>4</sub> and % CO <sub>2</sub> vs SRT	59
17	COD <sub>ins</sub> COD out and % COD Removal vs OLR	61
18	% COD Removal and SUR vs OLR	62
19	Permeate Flux vs Cumulative Days	66
20	Contois Model: SRT, S and E	73
21	Chen and Hashimoto Model: SRT, S and E	74
22	Monod Model: SRT. S and E	75



## LIST OF PLATES

	Plate	Page
1	The Sludge being Pushed Out Through the Gas Hose	. 41
2	The Original Reactor Content Level Prior Pumping Operation	42
3	The Sludge Foaming was Observed 20 Minutes Later after Introducing POME	42
4	Situation of Foaming Sludge at the Top Portion of Reactor	. 43
5	Unused Membrane with the Average Pore Size smaller than 1.0 µm	68
6	Used Membrane – most of the Pores were  Covered by Organic Substrates	. 68
7	Washed membrane – more Pores were Recovered but still surrounded by Organic Substrates	69



#### LIST OF ABBREVIATIONS

b Specific Microorganism Decay Rate

BLR Biological Loading Rate

COD Chemical Oxygen Demand

CSTR Completely Mixed Stirred Tank Reactor

E Substrate Utilisation Rate

HRT Hydraulic Retention Time

k Maximum Specific Substrate Utilisation Rate

θc Solids Retention Time (MCRT)

K<sub>s</sub> Half-velocity Coefficient

MAS Membrane Anaerobic System

MLSS Mixed Liquor Suspended Solids

MWCO Molecular Weight Cut-off

OLR Organic Loading Rate

POME Palm Oil Mill Effluent

PVC Polyvinylchloride

S Effluent Substrate Concentration

S<sub>o</sub> Influent Substrate Concentration

SEM Scanning Electrom Microscope

SRT Solids Retention Time

SS Steady State

SSUR Specific Substrate Utilization Rate

SUR Substrate Utilization Rate

TSS Total Suspended Solids

 $\mu$  Specific Growth Rate

 $\mu_{\rm m}$  Maximum Specific Growth Rate

VSS Volatile Suspended Solids

X Microorganism Concentration

Y Growth Yield Coefficient



Abstract of thesis presented to the Senate of Universiti Putra Malaysia in partial fulfilment of the requirements for degree of Master of Science

THE PERFORMANCE AND KINETIC STUDY OF MEMBRANE ANAEROBIC SYSTEM (MAS) IN TREATING POME

By

LAI LONG SENG

November 1999

Chairman:

coefficients.

Fakhru'l Razi Ahmadun, Ph.D.

Faculty:

Engineering

Anaerobic digestion has been proven to be the most efficient process for primary treatment of POME. However a major problem in the anaerobic wastewater treatment process is to maintain the sufficient quantity of active biomass in the reactor. In this study membrane separation technology has been applied after anaerobic digestion to increase solids retention time and improve treatment efficiency. The objectives of the study are to evaluate the overall membrane anaerobic system (MAS) treatment efficiency and the applicability of three known kinetic models on the system and determination of kinetic

The MAS consists of a cross-flow ultrafiltration membrane (PCI Micro 240) for solid-liquid separation. Six steady states were ottained over a range of mixed liquor suspended solids of 12,681 – 30,460 mg/l. The study showed a good fitting of the Monod Model (91.1%), Contois Model (98.5%) and Chen and Hashimoto Model (95%)

UPM

for the MAS treating raw POME at organic loadings between 1.5 kgCOD/m<sup>3</sup>/d to 6.5 kgCOD/m<sup>3</sup>/d. The growth yield coefficient, Y, was found to be 0.604 kg VSS/kgCOD while the specific microorganism decay rate was 0.099 day<sup>-1</sup>. The k values were in the range of 0.242 to 0.425 mg COD/mg VSS.d and the  $\mu_m$  values were between 0.145 to 0.257day<sup>-1</sup>. The Monod Model and Chen and Hashimoto Model are better than the Contois Model for solids retention time (SRT), effluent substrate concentration (S) and substrate utilisation rate (E) estimation. Both models are able to produce a good predicted S and E if the SRT  $\geq$  50 days. Throughout the study, the removal efficiency of COD was 83.2 to 97.97 %. The methane production rate was between 0.262 to 0.473 l/g-COD-utilised/d. The MAS treatment efficiency was greatly affected by SRT and OLRs. In this study, membrane fouling and polarization at the membrane surface played a significant role in the formation of a strongly attached cake layer limiting membrane permeability.



Abstrak tesis yang dikemukakan kepada Senat Universiti Putra Malaysia sebagai

memenuhi sebahagian keperluan untuk ijazah Master Sains

KAJIAN PRESTASI DAN KINETIK BAGI SISTEM ANAEROBIK MEMBRAN (MAS) DALAM PERAWATAN POME

Oleh

LAI LONG SENG

November 1999

Pengerusi:

Fakhru'l-Razi Ahmadun, Ph.D.

Fakulti:

Kejuruteraan

Pencernaan anaerobik telah dibukti sebagai proses yang paling berkesan dalam

rawatan POME. Bagaimanapun masalah utama yang dihadapi dalam rawatan air sisa

anaerobik ialah penahanan biojisim yang aktif serta mencukupi dalam reaktor. Dalam

pengajian ini teknologi membran telah diguna selepas pencernaan anaerobik demi

meningkat masa tahanan pepejal dan mempertingkatkan keberkesanan rawatan. Objektif-

objektif pengajian ialah menilai keberkesanan keseluruhan sistem rawatan anaerobik

membran (MAS) dan penggunaan tiga jenis model kinetik pada sistem serta penentuan

koefisien-koefisien kinetik.

Sistem ini terdiri daripada membran ultraturasan (PCI Micro 240) untuk

pemisahan pepejal-cecair. Enam tahap tetap telah dicapai untuk pepejal terampai larutan

campuran antara 12,681- 30,460 mg/l. Kajian menunjukkan kepadanan yang baik bagi

Model Monod (91.1%), Model Contois (98.5%) dan Model Chen dan Hashimoto (95%)

xii

untuk perawatan POME dengan MAS bagi muatan bebanan organik antara 1.5 kgCOD/m³/d dan 6.5 kgCOD/m³/d. Koefisien Penghasilan Pertumbuhan, Y ialah 0.604 kgVSS/ kgCOD manakala kadar penguraian makro-organisma ialah 0.099 hari¹. Nilainilai k adalah dalam julat 0.242 – 0.425 mg COD/ mgVSS.h dan nilai-nilai µm adalah dalam lingkungan 0.145 – 0.257 hari¹. Model Monod dan Model Chen dan Hashimoto didapati lebih baik dibanding dengan Model Contois bagi penganggaran masa penahanan pepejal (SRT), kepekatan substrak terawat (S) dan kadar penguraian substrak (E). Untuk kedua-dua model ini dapat menghasilkan anggaran baik untk ramalan S dan E jika SRT ≥ 50 hari. Sepanjang kajian ini, kecekapan penyingkiran COD berada pada 83.2 hingga 97.97 %. Kadar penghasilan metana berada pada 0.262 hingga 0.473 l/g-COD-penggunaan/ h. Kecekapan rawatan MAS amat dipengaruhi oleh SRT dan OLRs. Dalam kajian ini, penyumbatan membran dan polarisasi pada permukaan membran memainkan peranan yang penting dalam pembentukan lapisan kek yang melekat dengan kuatnya justeru menghadkan keronggaan membran.



#### **CHAPTER I**

#### INTRODUCTION

Anaerobic digestion has made considerable progress in the last two decades as a result of active research in this field. This technology is recognised as a versatile biological waste treatment particularly for treating high strength organic wastewater and solids concentration. Besides that the methane-rich biogas produced as a byproduct of the process is considered as a useful biofuel for power to offset the cost of the treatment.

In Malaysia, the palm oil industry is a very important agriculture-based industry. Currently there are more than 2.5 million hectares of land under oil palm cultivation and there are 280 palm oil mills and 36 active refineries (Ma, 1997). In 1994 however, besides producing 7.2 million tonnes of crude palm oil, the palm oil mills also generated about 18.0 million tonnes of palm oil mill effluent (POME) (Ma, 1995). Due to the highly polluting characteristics (Table 1) of POME, much efforts have be done to overcome this problem. In fact anaerobic digestion has been proven to be the most efficient process for primary treatment of POME and all palm oil mills have adapted this process to decrease environmental pollution (Ma, 1997).



However due to the slow growth rate of anaerobic microorganisms, therefore in this study, the combination of anaerobic treatment and membrane

Table 1: Typical Analysis of Palm Oil Mill Effluent

Parameter	Range	Mean
BOD <sub>3</sub> , 30°C	10,250-47,500	25,000
COD	15,500-106,360	53,635
Total Solids	11,450-164,950	43,635
Suspended Solids	410-60,360	19,020
Oil & Grease	130-86,430	8,370
Ammonical-N	0-110	35
pН	3.8-4.5	4.0

All parameters are expressed in mg/l except pH

Source: Ma and Hassan (1991)

separation technology will be investigated in treating palm oil mill effluent. In fact several investigators have conducted experimental works of anaerobic membrane processes for treatment of a variety of wastewater (Fakhru'l-Razi, 1994; Ross et al., 1992; Hall et al., 1995). In this study, the experiment is carried out under six steady states and the membrane anaerobic system (MAS) inherently allows the separation of hydraulic retention time (HRT) and solid retention time (SRT), thus increase the biomass retention period in reactor.

#### **Objectives**

The objectives of this study in treating the palm oil mill effluent are:

- 1. To evaluate the overall MAS treatment efficiency, and
- To evaluate the applicability of three known kinetic models on the system and determination of kinetic coefficients.



#### **CHAPTER II**

#### LITERATURE REVIEW

#### **Biological Treatment**

Biological treatment process has been widely used for wastewater treatment. In fact, it can be classified into two groups:

- Aerobic processes in which the microbes use oxygen dissolved in the waste liquors.
- Anaerobic processes in which the microorganisms do not have access to
  freely dissolved oxygen, nor to other energetically favorable electron
  acceptors such as nitrate ions. Microorganisms can use the carbon in organic
  molecules as the electron acceptor.

Comparison between aerobic and anaerobic processes for wastewater treatment has tended to the former because the system is more reliable, stable and better understood. However Lettinga (1996) concluded that the anaerobic processes have several clear advantages as:

- Treatment can be accomplished at very low costs, viz. the installations are relatively plain.
- Instead of consuming energy, a useful energy carrier in form of biogas is produced.



- The method can be applied at practically any place and at any scale.
- Very high space loading rates frequently can be applied in modern anaerobic wastewater treatment systems, so that the space requirements of the system are relatively small.
- The volume of excess sludge produced in anaerobic treatment generally is significantly lower compared to aerobic treatment. The excess sludge generally is well stabilized.
- Anaerobic organisms can be preserved unfed for long periods of time (exceeding one year) without any serious deterioration of their activity, while also other important characteristics of anaerobic sludge generally remain almost unaffected.
- The method can lead to the application of integrated environmental
  protection systems, e.g. it can be combined with post-treatment methods by
  which useful products like ammonia or sulfur can be removed, while in
  specific cases effluents and excess sludge could be employed for irrigation
  and fertilization or soil conditioning.

However the main disadvantages of anaerobic system is the lower rates of reaction when compared to aerobic processes. The growth rate of certain microorganisms in anaerobic processes is slightly lower but the high concentration of action biomass is an important factor in any successful treatment system. Thus the understanding of the kinetics microbiology and biochemistry of the anaerobic processes is essential in any engineering practice.



**Biochemistry and Microbiology** 

The understanding of biochemistry and microbiology mechanisms of anaerobic

digestion is important in process control and optimisation, especially during start-up

and for preventing digester instability. Basically the biological conversion of

complex macromolecules organic matter by anaerobic bacteria will pass through in

four steps, namely hydrolysis, acidogensis, acetogenesis and methanogenesis.

First step: Hydrolysis

In this process, it involves the enzyme-mediated transformation for higher-

molecular-mass compounds into compounds suitable for use as source of energy and

cell carbon (Metcalf & Eddy, 1991). Haandel and Lettinga (1994) also reported that

hydrolysis process involves the mediation of exo-enzyme that is excreted by

fermentation bacteria. Organic polymers and lipids are hydrolyzing to basic

structural building blocks such as monosaccharides, amino acids, fatty acids and

related compounds as shown in Figure 1. Hydrolysis is claimed to be rate-limiting

when the waste contains much insoluble material (Archer and Kirsop, 1991). In fact

at lower temperature (< 20 °C), and particular for lipids, hydrolysis rate practically

can be limiting for the overall rate of anaerobic digestion (Haandel and Lettinga,

1994).



Second Step: Acidogenesis

The acidogenic bacteria will ferment the breakdown products from hydrolysis to

simple organic acids, mainly volatile fatty acid, alcohols, lactic acid and mineral

compounds such as carbon dioxide, hydrogen, ammonia and hydrogen sulfide gas

(Haandel and Lettinga, 1994). The responsible organisms are called "acid-

producing" or "acid-forming" bacteria. In fact acidogens and hydrolysis bacteria are

considered as one group in Sahm (1984). Metcalf and Eddy (1991) and Sahm (1984)

reported that members of this group may be either strict anaerobes or facultative. It is

believe that the concentration of hydrogen plays a central role in controlling the

proportions of the various products from acidogenic bacteria and the acidogenic

bacteria may utilize feedback control loops to stabilize the digester stability (Sahm

1984).

Third Step: Acetogenesis

The hydrogen producing acetogenic bacteria which include both obligate and

facultative species can ferment organic acids larger than acetic (e.g. butyrate,

propionate) and neutral compounds larger than methanol (e.g. ethanol, propanol) to

hydrogen and acetate (Zeikus, 1981). Besides that the homoacetogenic bacteria can

ferment a very wide spectrum of multi or one carbon compounds to acetic acids. By

consuming hydrogen, homoacetogenisis lower the hydrogen partial pressure in

anaerobic digestion (Zeikus, 1981). In fact the conversion of various fermentation

products by obligate hydrogen producing bacteria can only be functioning if the



partial pressure of hydrogen is kept low by hydrogen consuming organism (Zehnder et al., 1981).

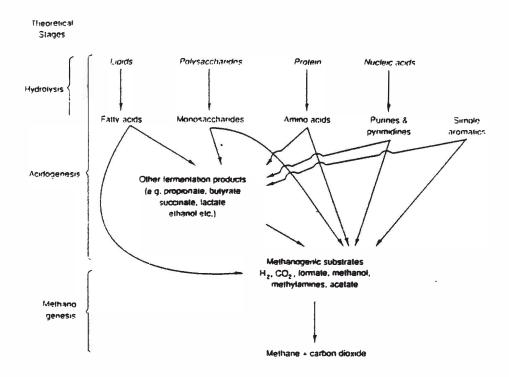


Figure 1: Schematic Diagram of the Patterns of Carbon Flow in Anaerobic Digestion (Metcalf & Eddy, 1991)

#### Fourth Step: Methanogenesis

In this process, hydrogen and acetate acid are converted to methane gas and carbon dioxide. The bacteria responsible for conversion are strictly anaerobes and these methanogenic bacteria are physiologically united by their requirement to form methane as final product of energy metabolism (Sahm, 1984). The growth rate of methanogenic is lower than the acid-forming bacteria, thus it takes more time for the methane bacteria to recover from inhibition or shock conditions (Corbitt, 1998). As a result their metabolism usually considered as rate limiting in the anaerobic treatment



of organic waste (Metcalf and Eddy, 1991) as high treatment efficiencies can be only achieved as long as a sufficient quantity of active methanogens exist in the digester (Ince et al., 1995 and Ince et al., 1997). Methanogenic bacteria can only use a limited number of substrate for the formation of methane and the typical energy-yielding conversions of these substrates are as follow (Metcalf and Eddy, 1991):

Hydrogen 
$$4H_2 + CO_2$$
  $CH_4 + 2H_2O$ 

Acetate  $4 \text{ HCOOH}$   $CH_4 + 3CO_2 + 2H_2O$ 

Formate  $CH_3COOH$   $CH_4 + CO_2$ 

Methanol  $4CH_3OH$   $3CH_4 + CO_2 + 2H_2O$ 

Trimethylamine  $4(CH_4)_3N + H_2O$   $9CH_4 + 3CO_2 + 6H_2O$ 

The two principal pathways involved in methane formation (Figure 2) are:

- 1. The conversion of hydrogen and carbon dioxide to methane and water;
- 2. The conversion of acetate to methane and carbon dioxide.

The methanogens are able to utilize the hydrogen produced by the acidegens because of their efficient hydrogenase. The utilisation of the hydrogen by methanogens bacteria is termed as interspecies hydrogen transfer and it remove compounds that would inhibit the growth of acidogens (Metcalf and Eddy, 1991).

According to Sahm (1984), most methanogenic bacteria prefer to oxidize H<sub>2</sub> and reduce CO<sub>2</sub> to form methane as their pathway of methanogenesis. Contrary to hydrogen, acetate is a poor substrate and the slow growth rates for acetotropic methanogenesis might be a consequence of this fact (Zehnder et al., 1981) and so far



only three acetotropic methanogenic species (Methanosarsina barkeri, Methanococcus mazei and Methanothrix soehgenii) have been isolated in pure culture (Sahin, 1984). Thus, acetotropic methanogenesis are usually rate limiting, as their growth rate is much lower than hydrogenotrophs (Haandel and Lettinga, 1994).

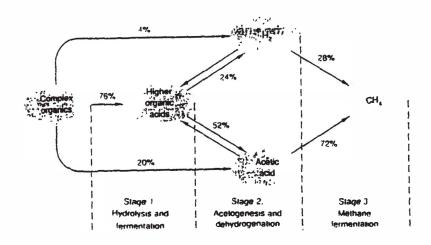


Figure 2: Steps in the Anaerobic Digestion Process with Energy Flow (Metcalf & Eddy, 1991)

#### Methane fermentation phase is the most important phase because:

- It is the only mechnism of BOD and COD removal. Waste stabilization in anaerobic is accomplished when methane and carbon dioxide is produced (Cheremisinoff, 1994a).
- 2. The reproduction rate for methane bacteria is low relative to other groups of bacteria. The doubling time for acidogenisis is few hour while methanogenisis under ideal condition is four days (Cheremisinoff, 1994a).
  Thus this step have been found to be the rate-limiting step.



 Methanogenic bacteria are too sensitive to surrounding conditions changes compared to other anaerobes.

#### **Anaerobic Digestion**

The two types of commonly used anaerobic digesters are identified as standard-rate and high-rate reactor (Figure 3). In the standard-rate digestion process, the content of digester are usually unmixed and unheated and the detention times vary from 30 to 60 days (Metcaft and Eddy, 1991). In high-rate digester the mixing is continuous; thus the mixing provides better contact between the seeded sludge and fresh solids that have been added. Hence high-rate detention time normally is 15 days or less (Metcalf and Eddy, 1991). A combination of these two processes is known as the "two-stage process".

Several treatment systems have been developed by the palm oil industry in Malaysia. Due to the POME high organic content, it is easily amenable to biodegradation. Therefore the treatment system for POME consists essentially of anaerobic and aerobic or combination of this two biological processes. Ma and Hassan (1991) reported that the three most common and efficient wastewater treatment systems adopted by palm oil industry are ponding system, open tank digester with extended aeration and closed tank digester with biogas recovery and land application (Figure 4).



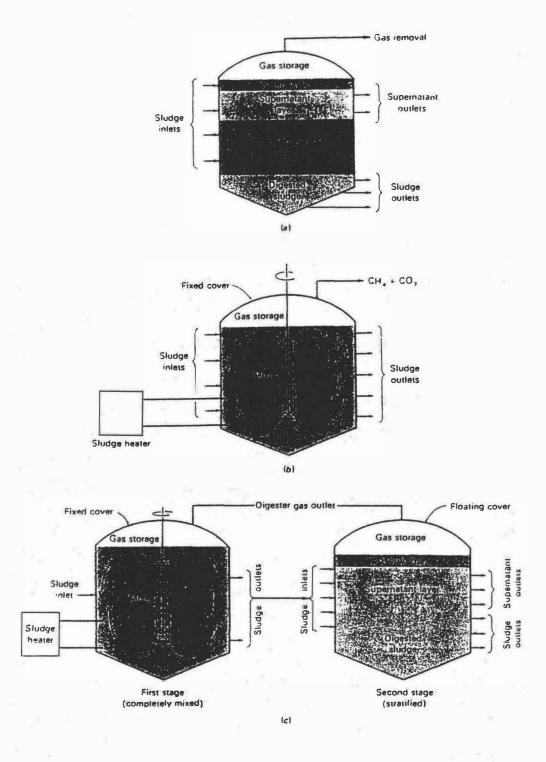


Figure 3: Typical Anaerobic Digestion: (a) Conventional Standard-rate Single-stage Process, (b) High-rate Complete-mix, Single-stage Process, and (c) Two-stage Process (Mecalf & Eddy, 1991)

